

# DES and AES

Chun-Jen Chung

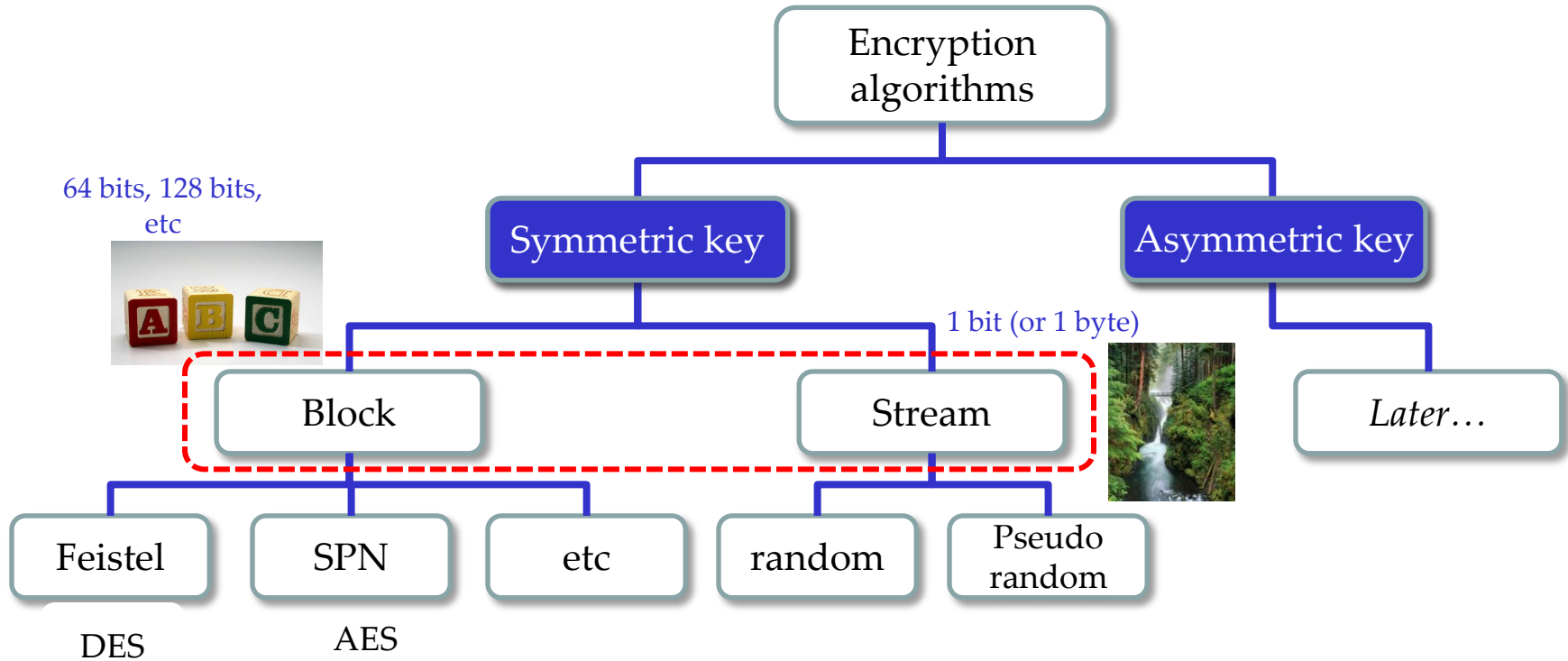
- Q: Why does the ciphers introduced so far not secure?
- A: because of **language characteristics**
- Q: Any ideas to improve them (you already know the answer)?
- A: Use both substitution and transposition

# From classical to modern ciphers

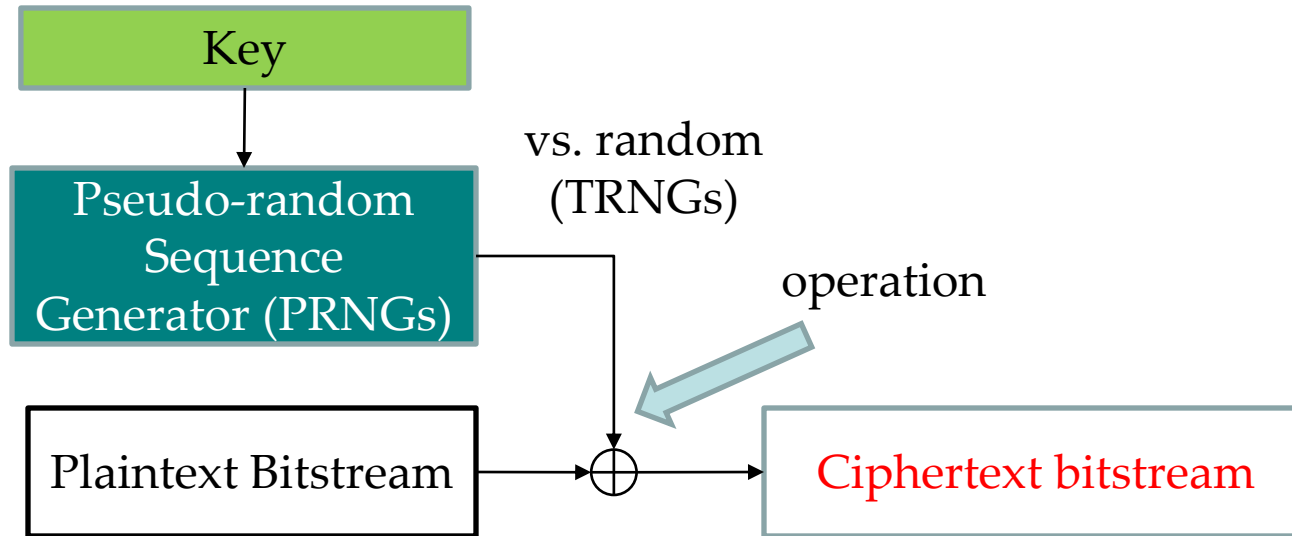
- Consider using several ciphers in succession to make harder, but:
  - Two substitutions make a more complex substitution
  - Two transpositions make more complex transposition
  - But a substitution followed by a transposition makes a new much harder cipher
- Q: What is this type of ciphers called?
- A: **product** ciphers
- This is *bridge* from classical to modern ciphers

- Q: What is most well-known and widely used modern cipher(s)?
- A: DES, AES,...

# Classification of encryption algorithms



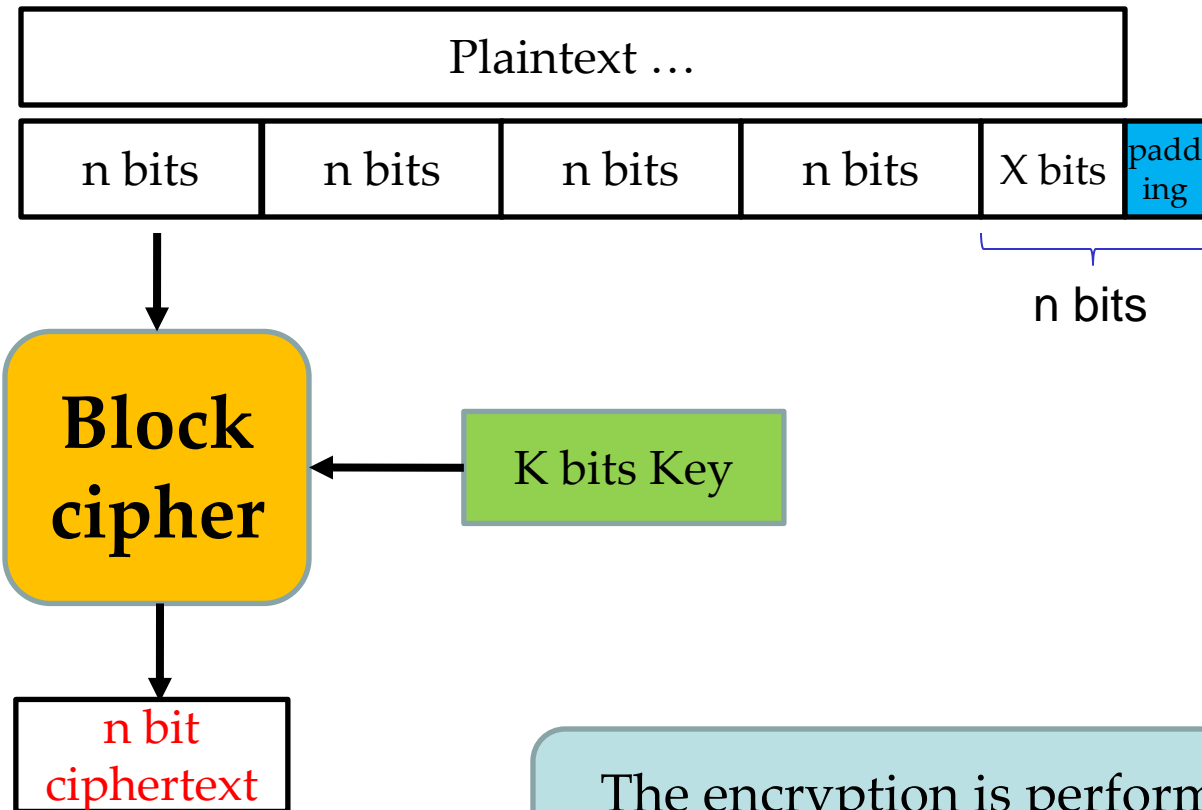
# Stream cipher



Plaintext bitstream	1 1 1 1 1 1 1 0 0 0 0 0 0 0 ...
Pesudo-random stream	1 0 0 1 1 0 1 0 1 1 0 1 0 0 ...
Ciphertext stream	0 1 1 0 0 1 0 1 1 1 0 1 0 0 ...

Q: Caesar is a stream cipher?

# Block cipher



The encryption is performed using one of the operation modes, we will visit it later.

Common block sizes:  
 $n = 64, 128, 256$  bits

Common key sizes:  
 $k = 40, 56, 64, 80, 128, 168, 192, 256$  bits

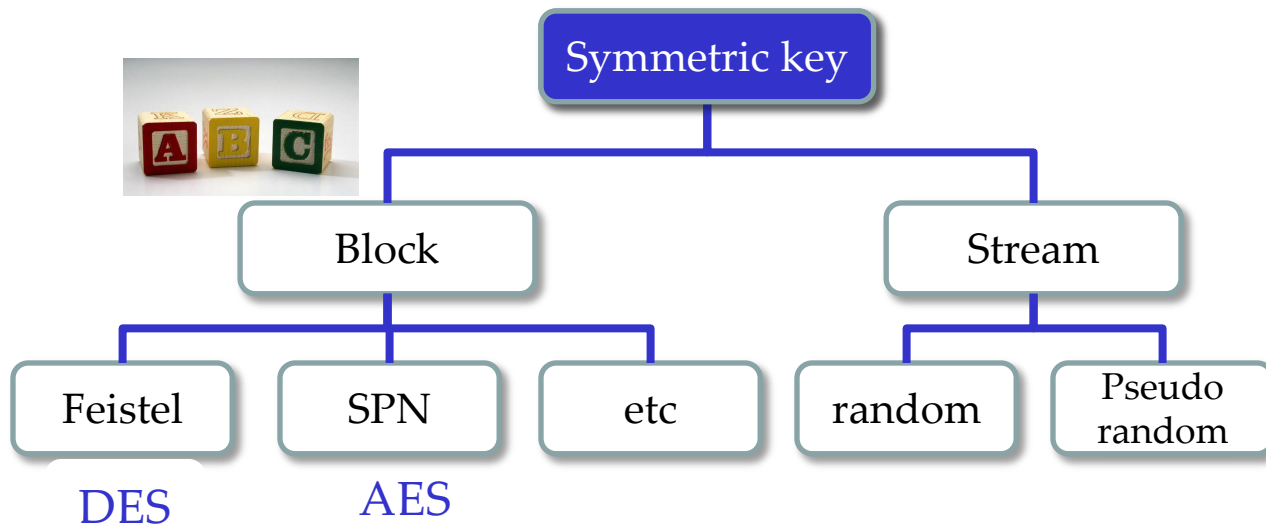
# Stream cipher vs. Block cipher

	Stream cipher	Block cipher
Pros.	<ul style="list-style-type: none"><li>• <b>Speed of transformation:</b> Because each symbol is encrypted without regard for any other plaintext symbols, each symbol can be encrypted as soon as it is read.</li><li>• <b>Low error propagation:</b> Because each symbol is separately encoded</li></ul>	<ul style="list-style-type: none"><li>• <b>High diffusion:</b> Information from the plaintext is diffused into several ciphertext symbols.</li><li>• <b>Immunity to insertion of symbols:</b> Because blocks of symbols are enciphered, it is impossible to insert a single symbol into one block. The length of the block would then be incorrect</li></ul>
Cons.	<ul style="list-style-type: none"><li>• Low diffusion</li><li>• Susceptibility to malicious insertions and modifications</li></ul>	<ul style="list-style-type: none"><li>• Slowness of encryption (c.f. faster than public key)</li><li>• Error propagation</li></ul>



# DES (Data Encryption Standard)

# Block cipher: DES, AES

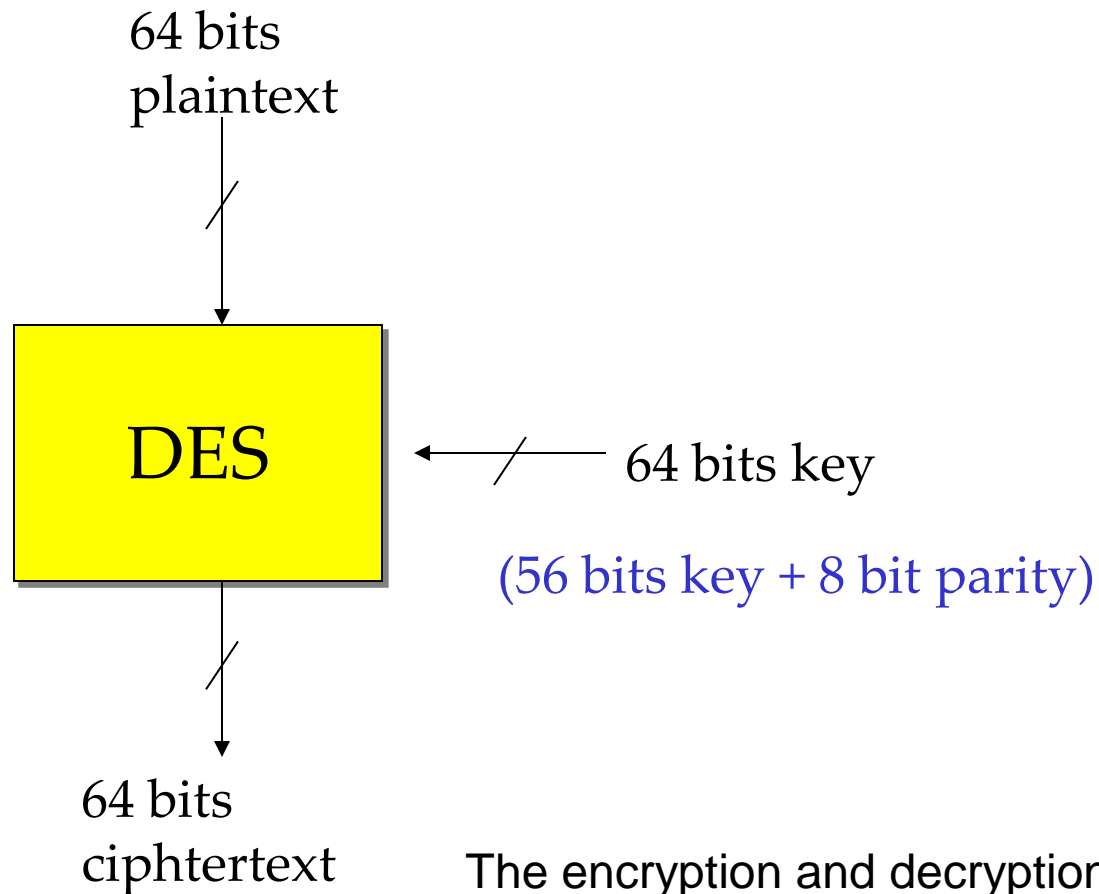


DES: Data Encryption Standard (1970s)  
or

DEA: Data Encryption Algorithm

AES: Advanced Encryption Standard (2001)

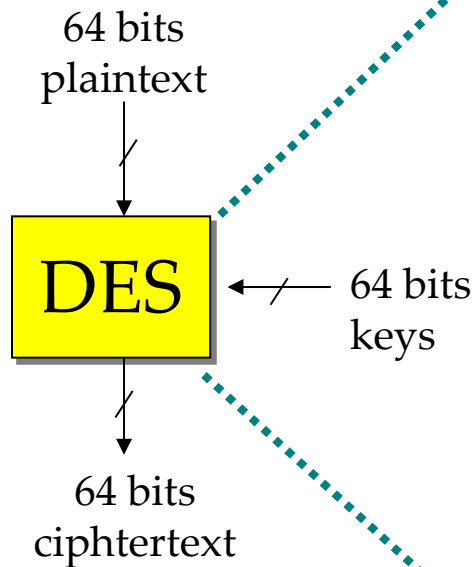
# DES Structure



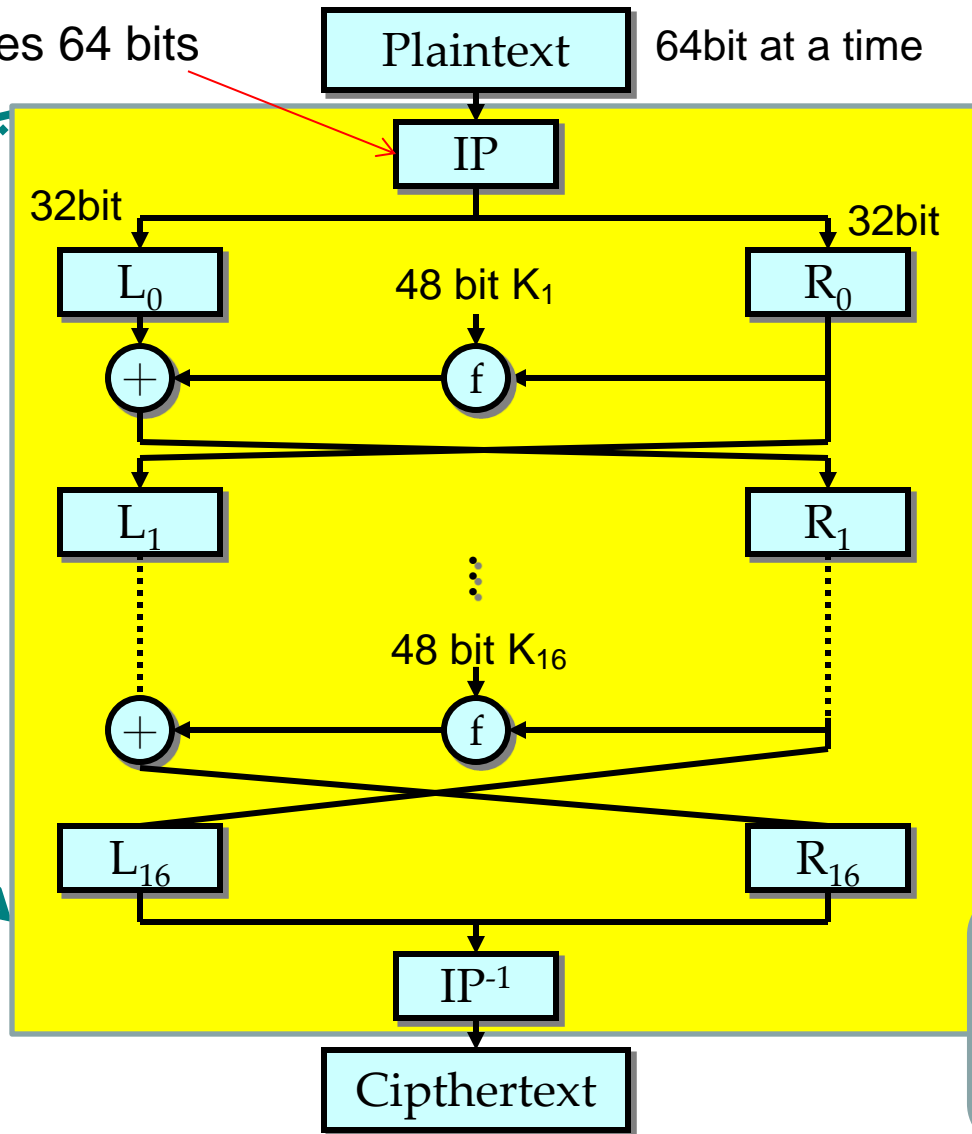
The encryption and decryption operations are very similar, even identical in some cases, requiring only a reversal of the key schedule.

# DES Structure

Initial permutation rearranges 64 bits  
(no cryptographic effect)



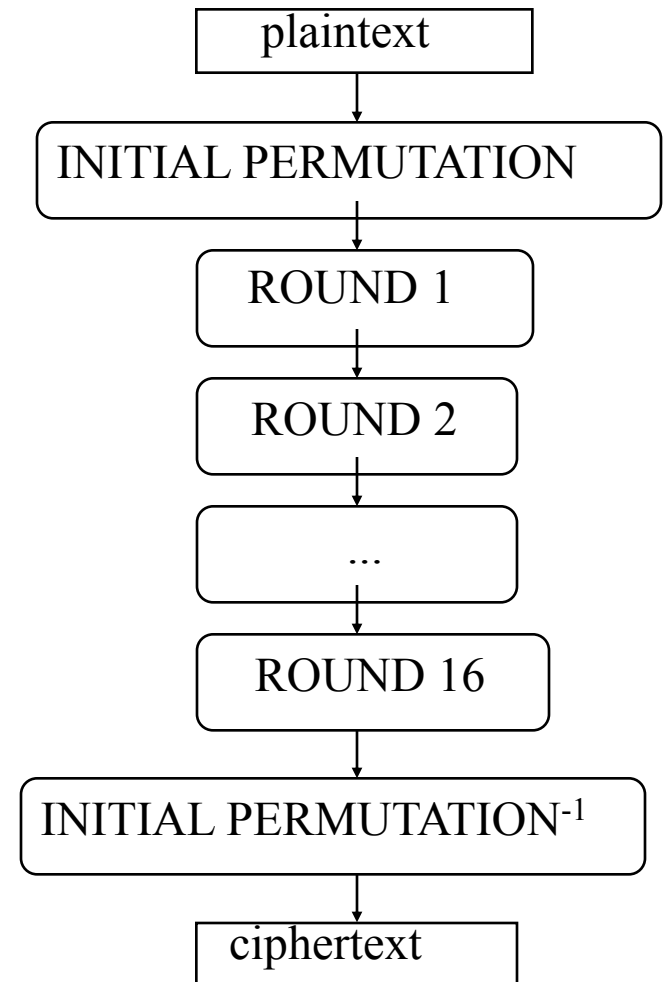
$$\begin{aligned}
 IP(M) &= L_0 R_0 \\
 L_i &= R_{i-1} \\
 R_i &= L_{i-1} \oplus f(R_{i-1}, K_i) \\
 C &= IP^{-1}(R_{16} L_{16}) \\
 1 \leq i \leq 15
 \end{aligned}$$



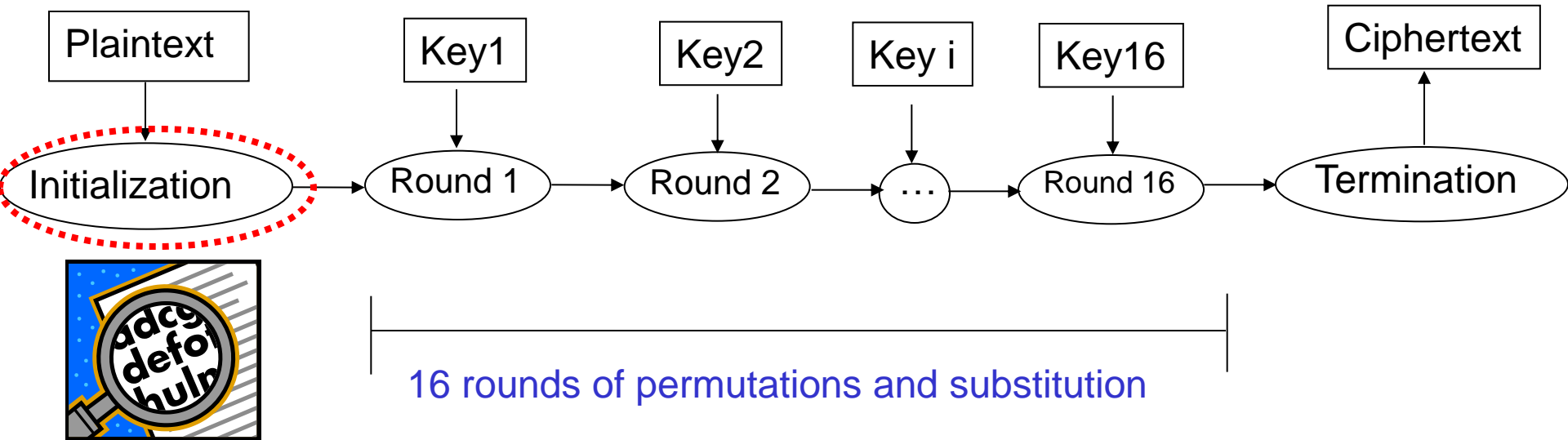
16  
rounds of  
permutations  
and  
substitution

# Overview of DES

- Block cipher: 64 bits at a time
- Initial permutation rearranges 64 bits (no cryptographic effect)
- Encoding is in 16 rounds



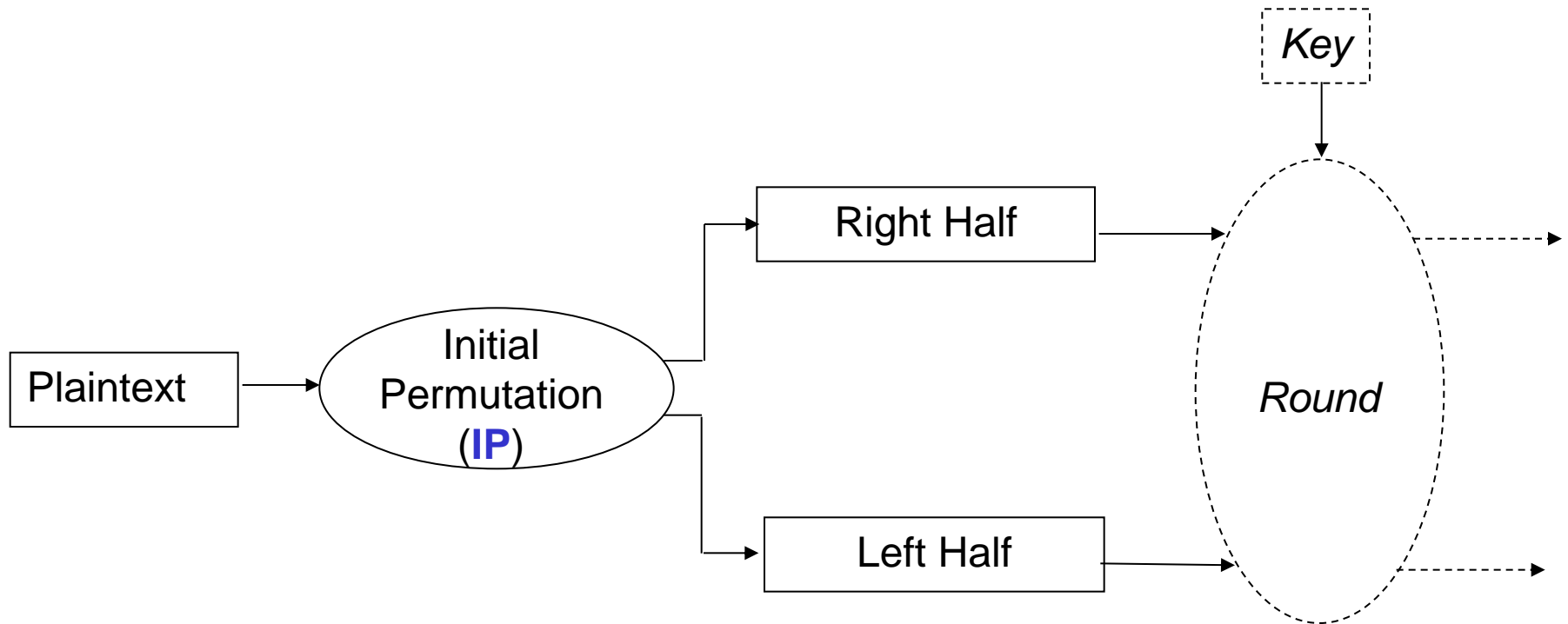
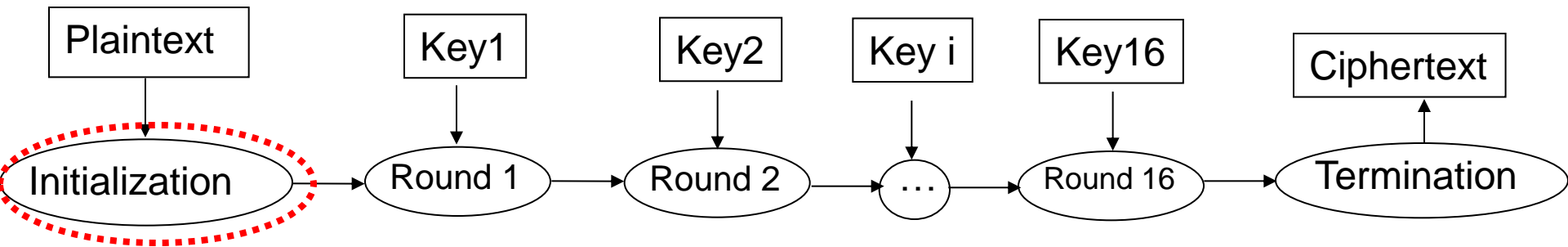
# Overview of DES



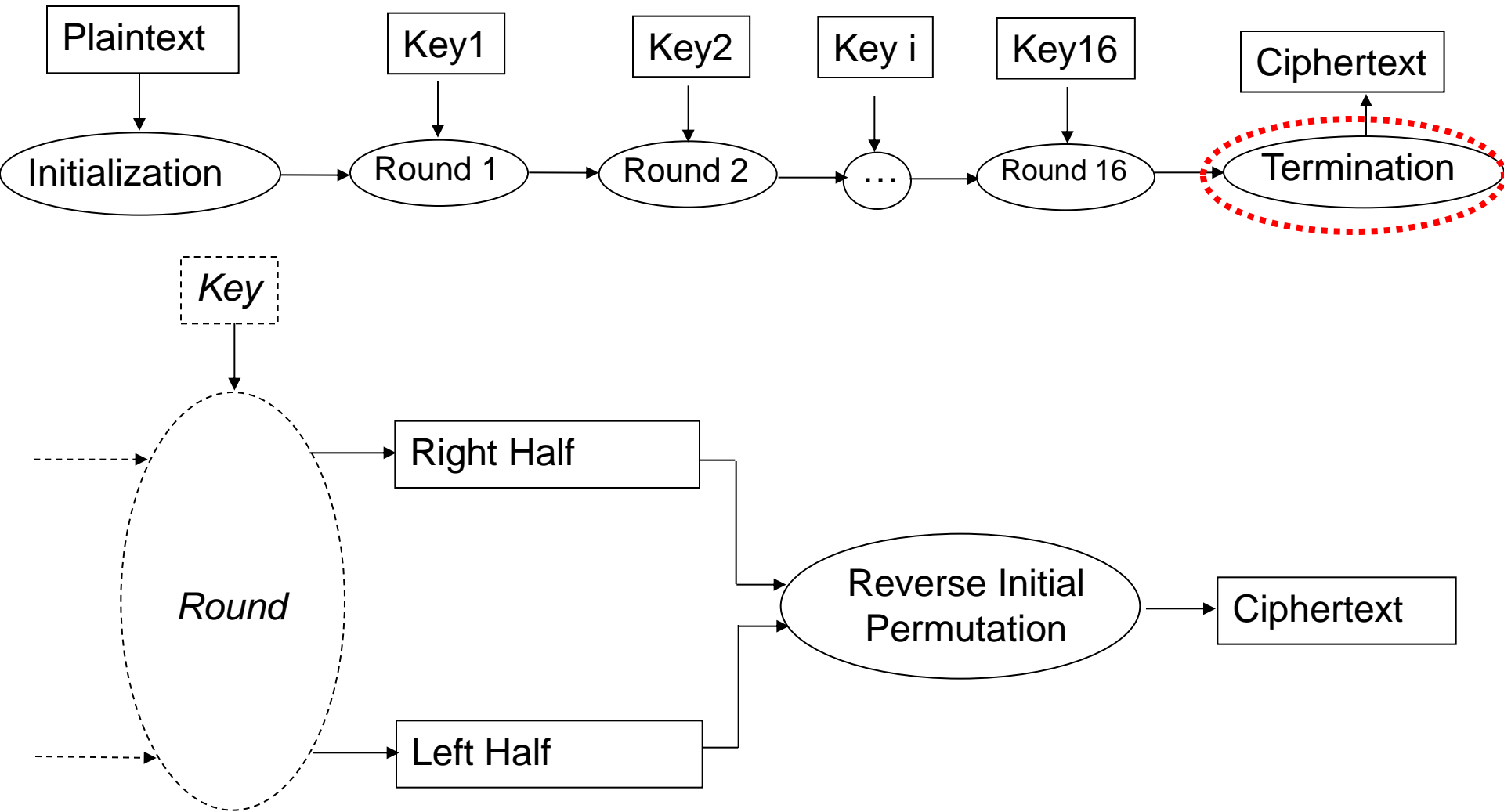
DES is a 64-bit block cipher. Both the plaintext and ciphertext are 64 bits wide.

The key is 64-bits wide, but every eighth bit is a parity bit yielding a 54-bit key.

# Initialization

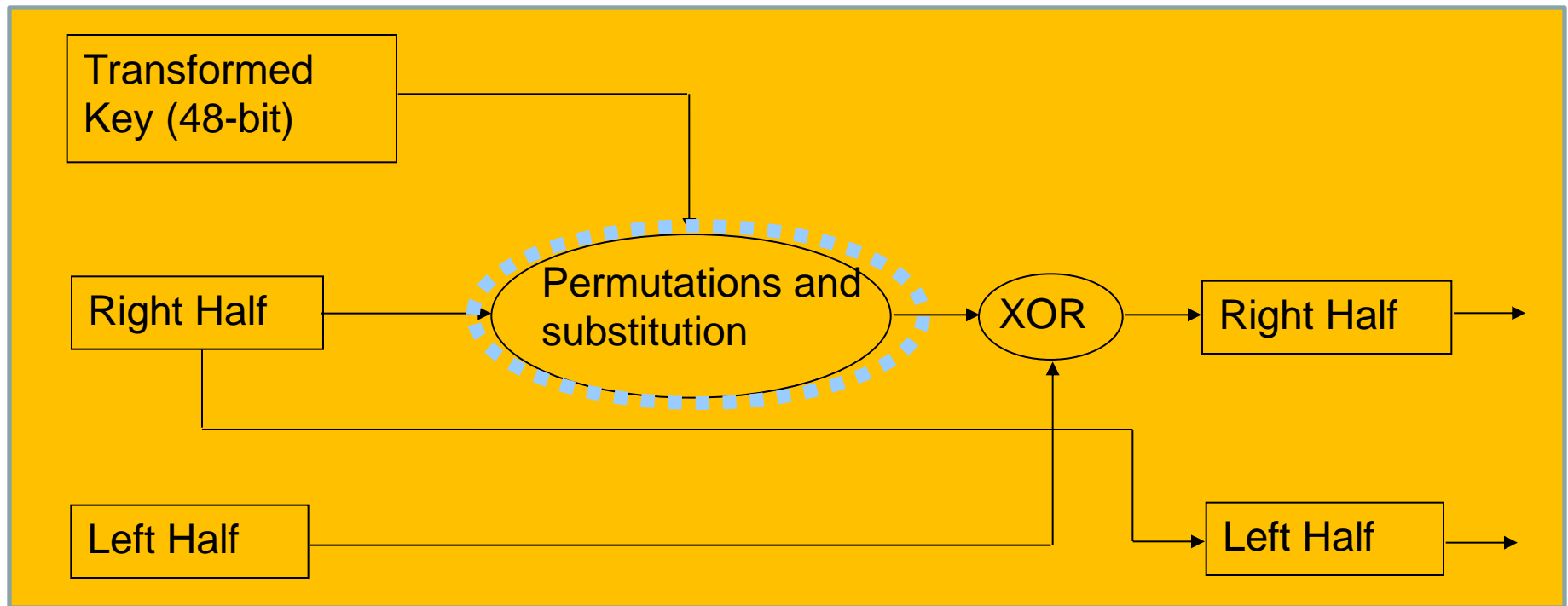
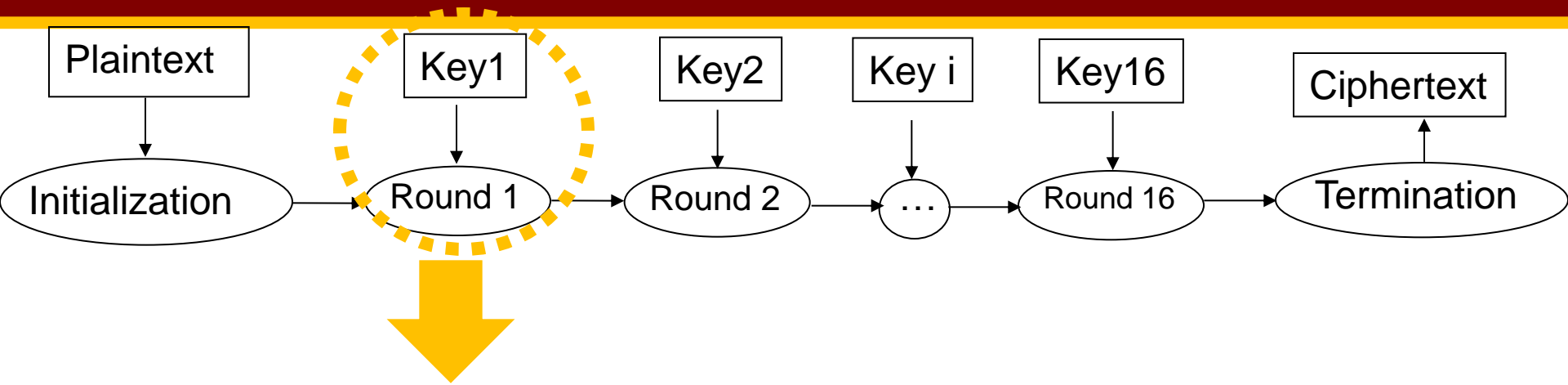


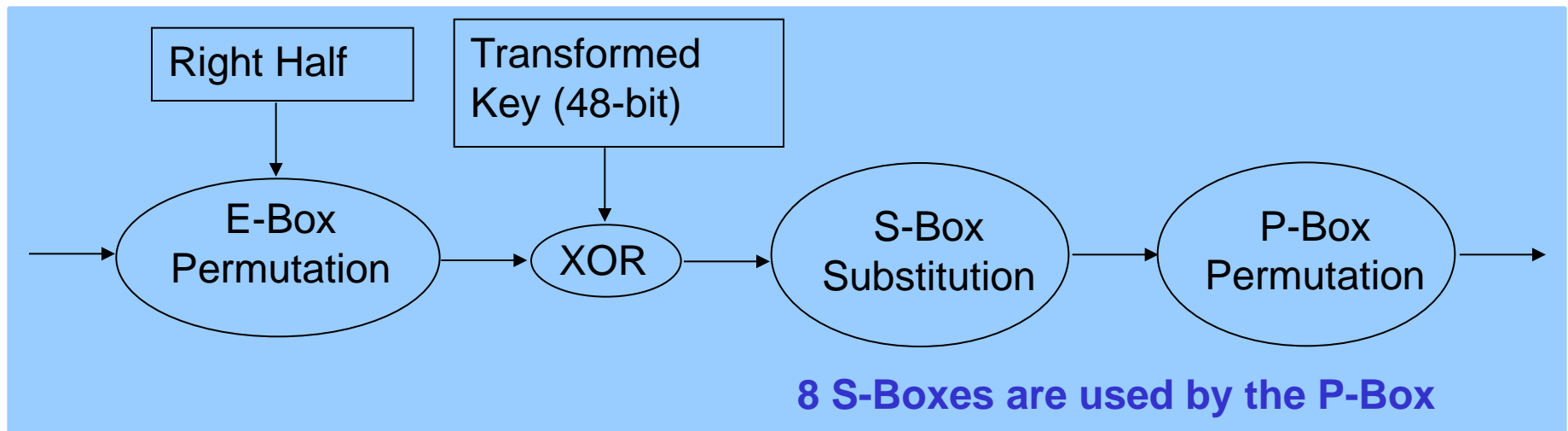
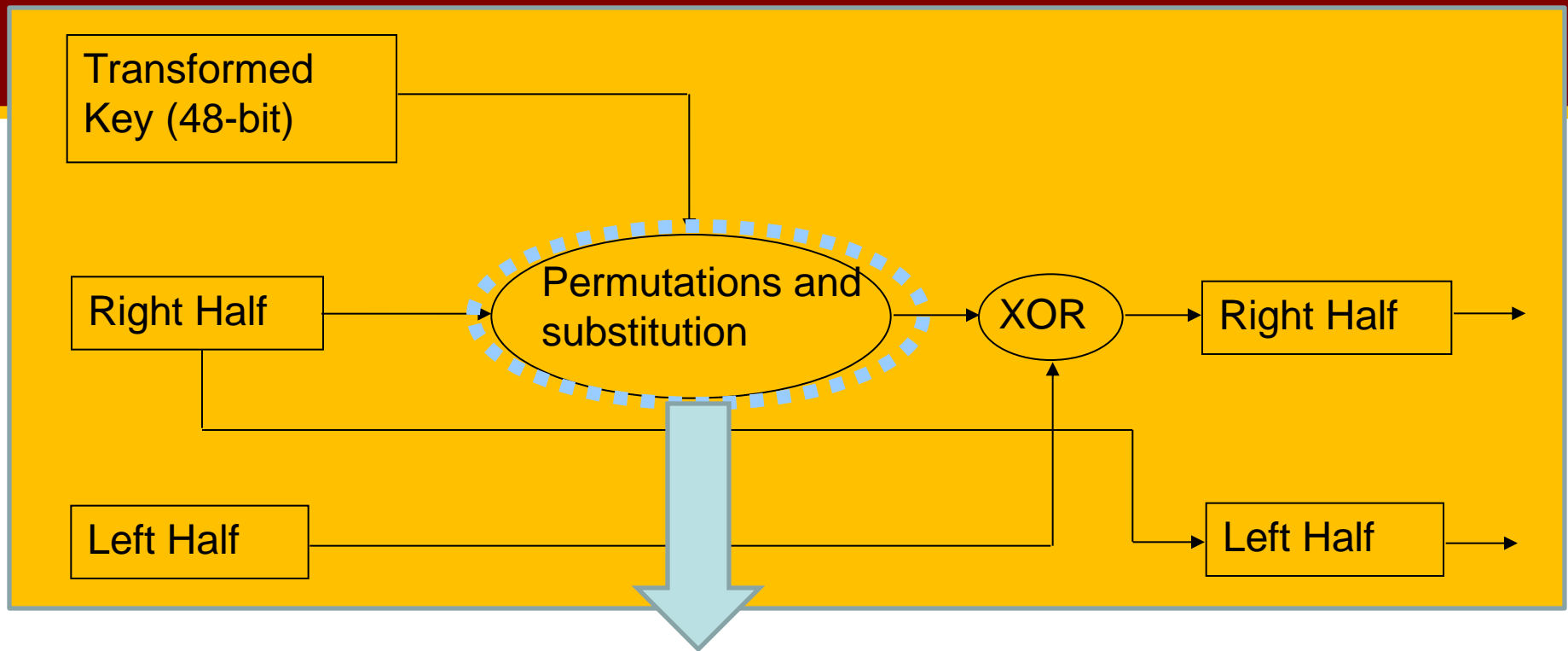
# Termination





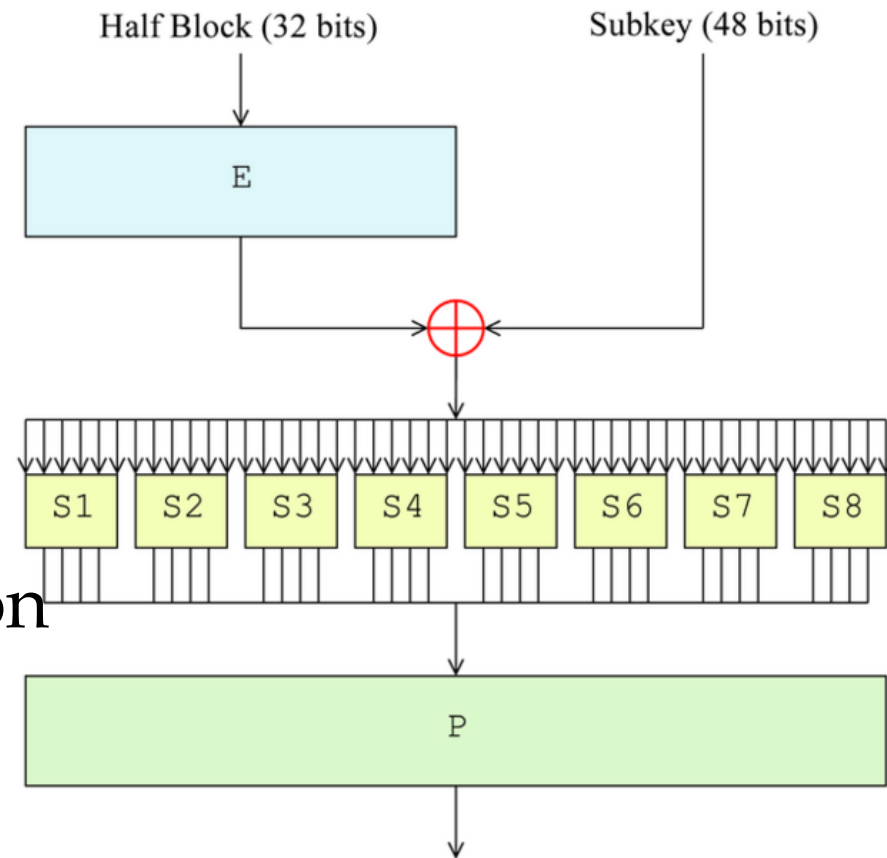
# A round





# Feistel Function (f function)

- E-box
  - Expansion permutation  
32-bits  $\rightarrow$  48-bits
- Key mixing
  - XOR with 48-bits subkey
- S-boxes (substitution)
  - Non-linear transformation
- P-box (permutation)
  - Rearrange output  
with fixed permutation function



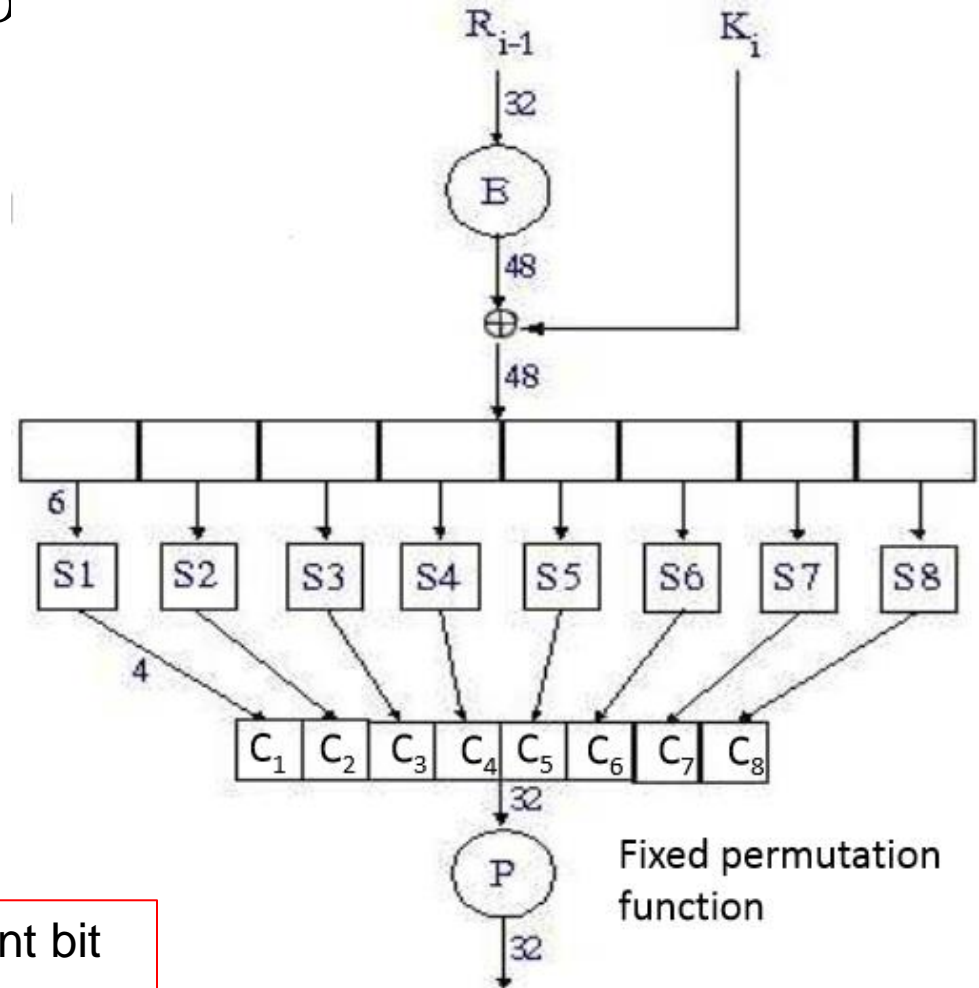
# E-box

## ■ Expansion function

- 32 bits  $\rightarrow$  48 bits

$S_1$	32	1	2	3	4	5
$S_2$	4	5	6	7	8	9
$S_3$	8	9	10	11	12	13
$S_4$	12	13	14	15	16	17
$S_5$	16	17	18	19	20	21
$S_6$	20	21	22	23	24	25
$S_7$	24	25	26	27	28	29
$S_8$	28	29	30	31	32	1

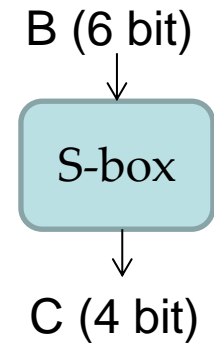
Add a copy of the immediately adjacent bit  
16 bits appear twice, in the expansion



# S-box

- Only *non-linear transformation* in DES, the core of security of DES.

- $B = b_1b_2b_3b_4b_5b_6$ 
  - $b_1b_6 \rightarrow \text{row } (2^2: 0\sim 3)$
  - $b_2b_3b_4b_5 \rightarrow \text{column } (2^4: 0\sim 15)$



- $C = S(\text{row}, \text{column})$

- E.g.

$B = 101111$

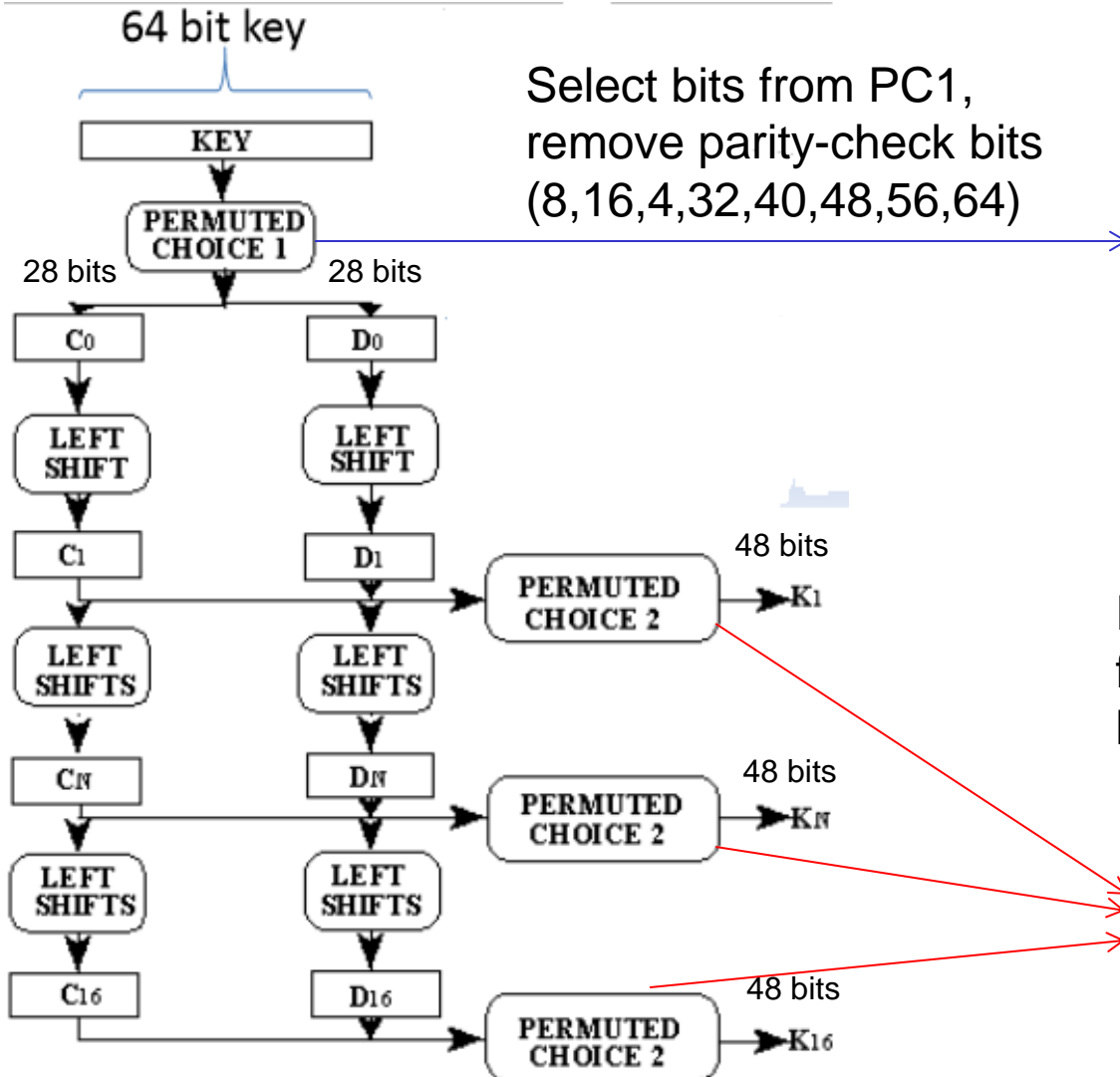
$C = S(3, 7) = 7$

$= \underline{0111}$

- $B = 011011, C = ?$

	$S_1$	1	2	3	...	<b>7</b>										15	
0	14	4	13	1	2	15	11	8	3	10	6	12	5	9	0	7	
1	0	15	7	4	14	2	13	1	10	6	12	11	9	5	3	8	
2	4	1	14	8	13	6	2	11	15	12	9	7	3	10	5	0	
<b>3</b>	15	12	8	2	4	9	1	<b>7</b>	5	11	3	14	10	0	6	13	

# DES Key Generation

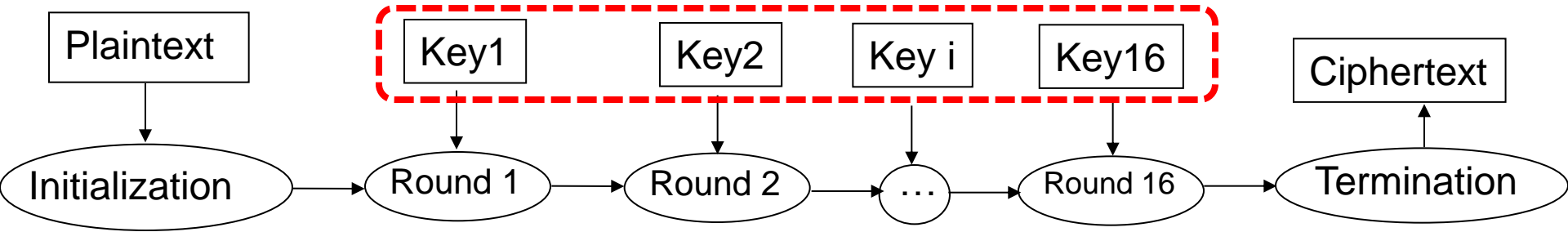


Left						
57	49	41	33	25	17	9
1	58	50	42	34	26	18
10	2	59	51	43	35	27
19	11	3	60	52	44	36
Right						
63	55	47	39	31	23	15
7	62	54	46	38	30	22
14	6	61	53	45	37	29
21	13	5	28	20	12	4

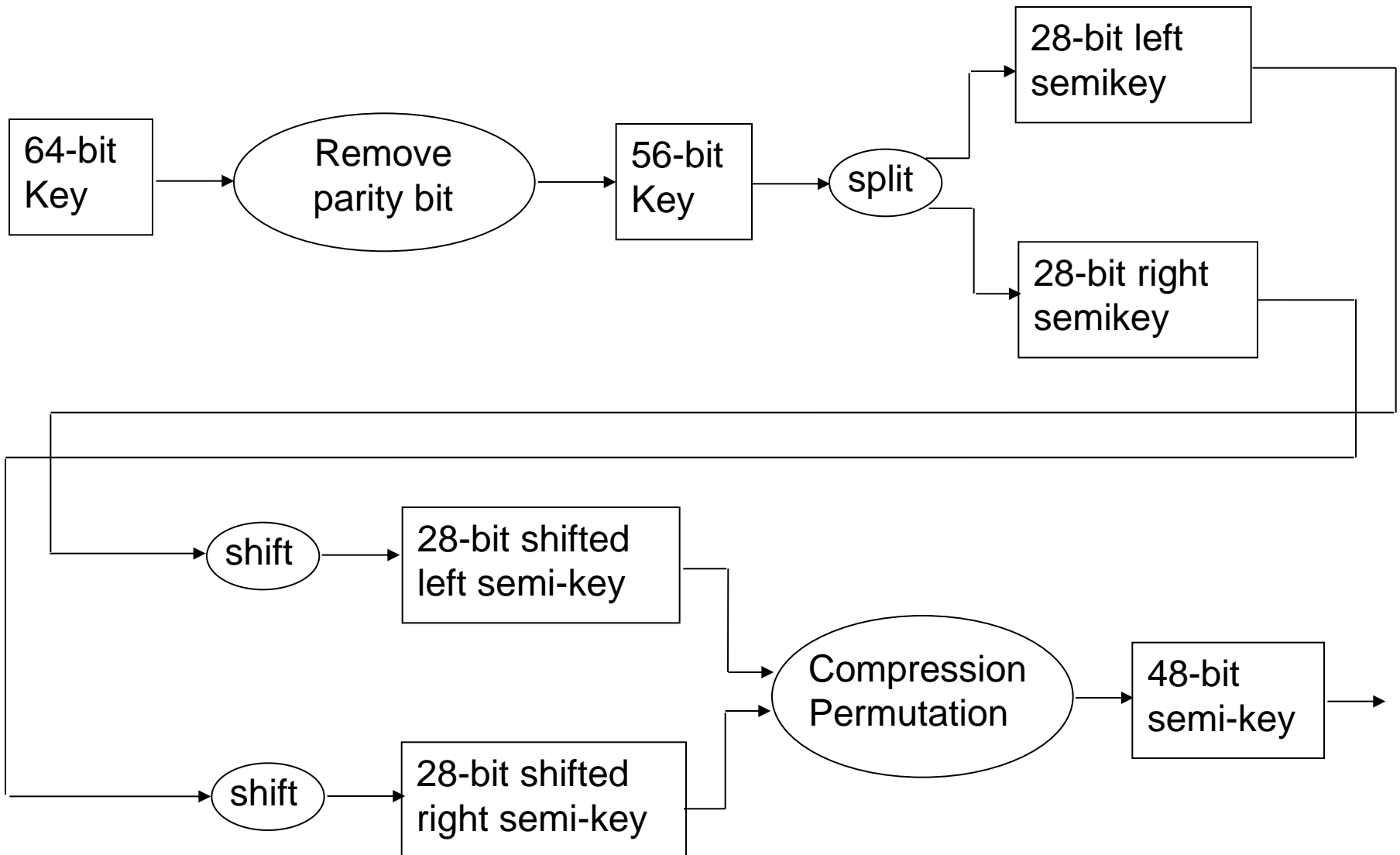
PC-2 selects the 48-bit subkey for each round from the 56-bit key-schedule state

14	17	11	24	1	5	3	28
15	6	21	10	23	19	12	4
26	8	16	7	27	20	13	2
41	52	31	37	47	55	30	40
51	45	33	48	44	49	39	56
34	53	46	42	50	36	29	32

# Key transform



# Key transform





# Study simple DES

- 8 bits block with a 10 bits key
- The encryption process is :
  - Initial Permutation
  - Function  $f_{k1}$
  - Switch of the key halves
  - Function  $f_{k2}$
  - Final Permutation (inverse of initial permutation)

# DES: security concern

- 56 bit key is too short
  - Can be broken on average in  $2^{55} \approx 3.6 \cdot 10^{16}$  trials
  - Moore's law: speed of processor doubles per 1.5 yr
  - 1997: 3500 machines broke DES in about 4 months
  - 1998: 1M dollar machine broke DES in about 4 days
  - ...

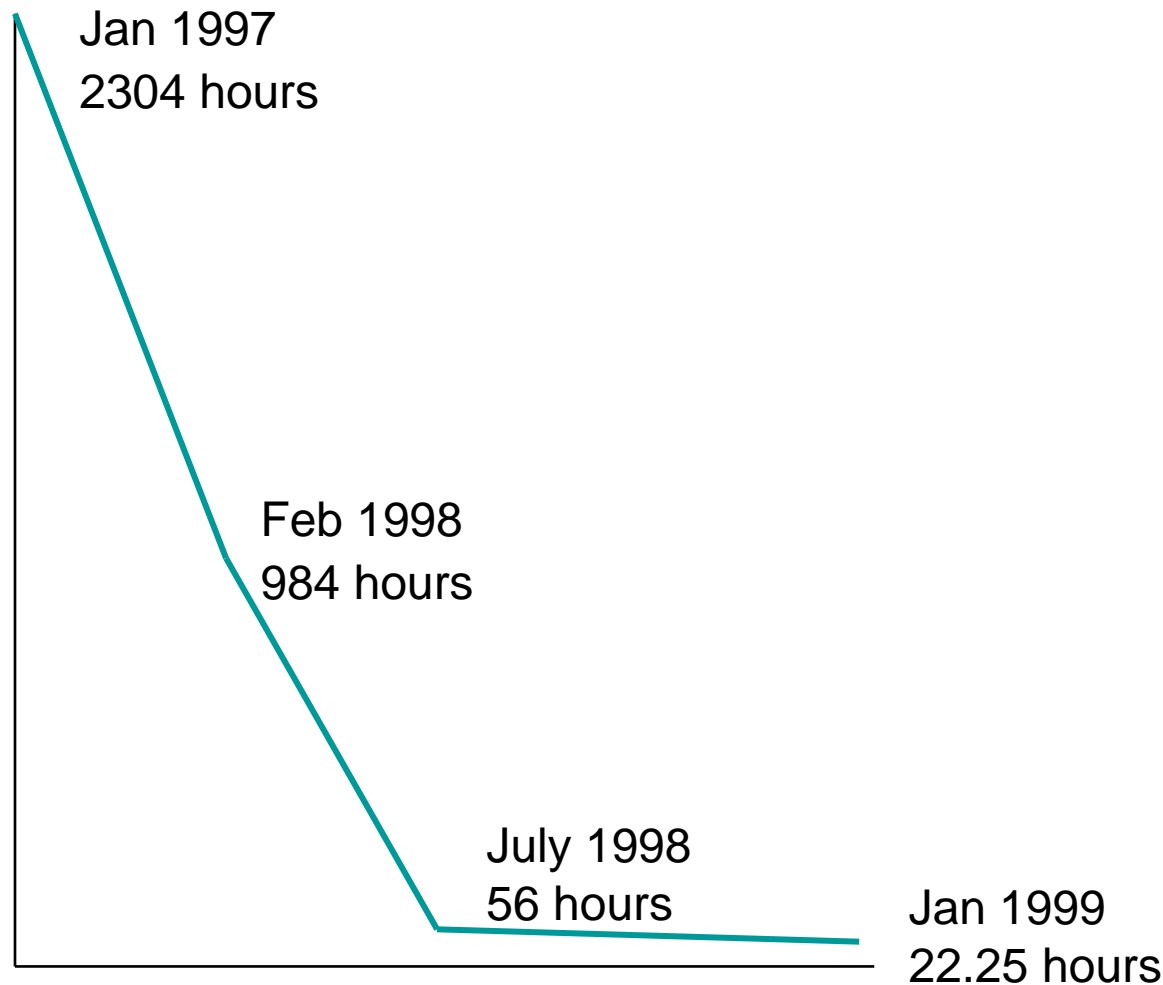
# DES: security concern

## ■ Weak Keys

- 56 bit key is too short
  - Can be broken on average in  $2^{56} \approx 7.21 \times 10^{16}$  trials
  - Moore's law: speed of processor doubles per 1.5 yr
- Keys make the same sub-key in more than 1 round.
- DES has 4 weak keys
  - 01010101 01010101
  - FEFEFEFE FEFEFEFE
  - E0E0E0E0 F1F1F1F1
  - 1F1F1F1F 0E0E0E0E
  - Using weak keys, the outcome of the PC1 to sub-keys being either all 0, all 1, or alternating 0-1 patterns.
  - Another problem:  $E_{\text{weak-key}}(E_{\text{weak-key}}(x)) = x$ .

# DES: security concern

- Cracking the 56-bit DES Encryption Algorithm



# Multiple Encryption & DES

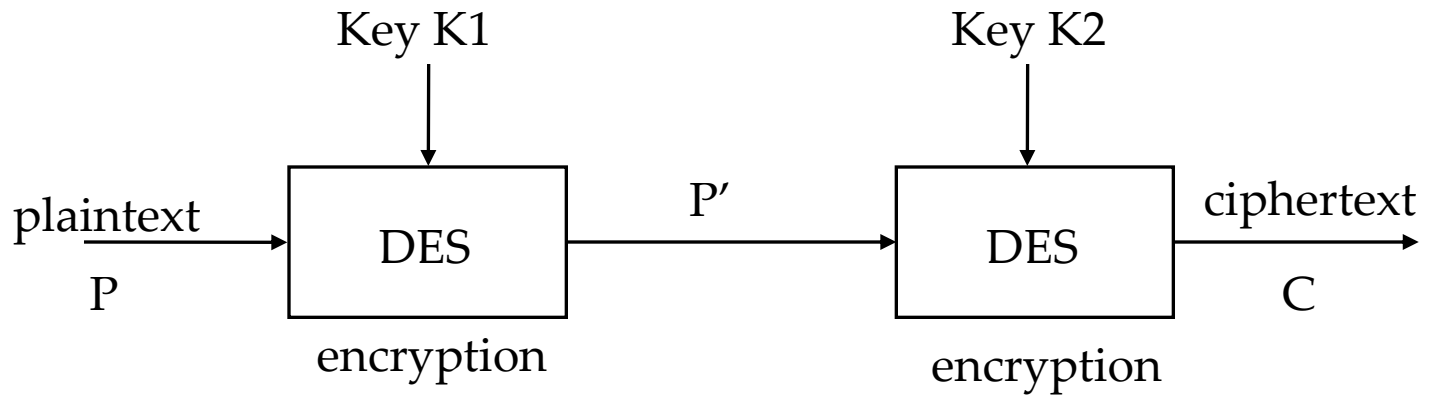
- DES is not secure enough.
- The once large key space,  $2^{56}$ , is now too small.
- In 2001, NIST published the **Advanced Encryption Standard (AES)** as an alternative.
- But users in commerce and finance are not ready to give up on DES.
- **Solution: to use multiple DES with multiple keys**

**Q: how many times can we use?**

**A: 2, 3, ...**

# Double-DES

- 2-DES



$$P' = E_{K1}(P)$$

$$P = D_{K1}(C')$$

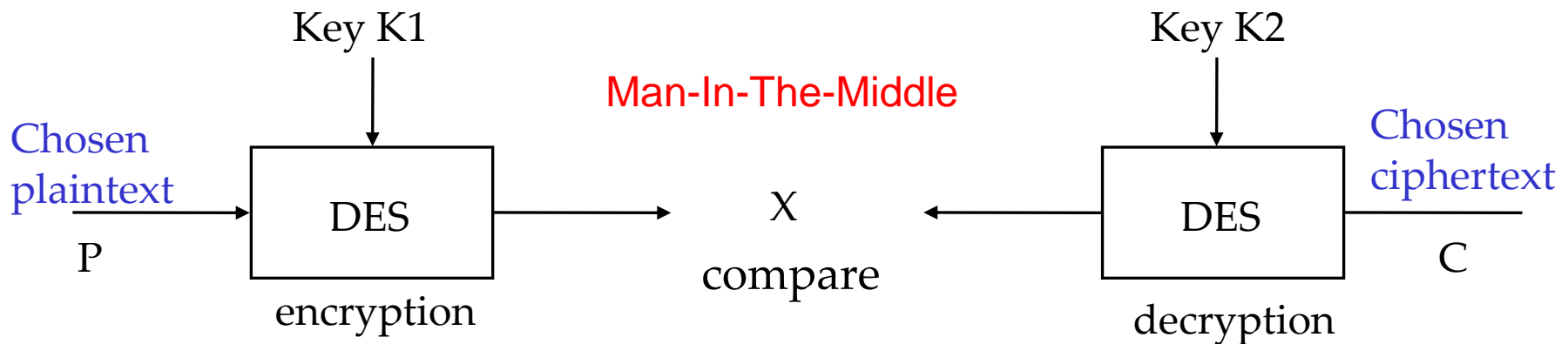
$$C = E_{K2}(P')$$

$$C' = D_{K2}(C)$$

Any problem for this scheme?

# Attack Double-DES

- 2-DES:  $C = E_{K2}(E_{K1}(P))$  ,  $P = D_{K1}(D_{K2}(C))$
- So,  $X = E_{K1}(P) = D_{K2}(C)$



(1) try all  $2^{56}$  possible keys for K1

(2) try all  $2^{56}$  possible keys for K2

(3) If  $E_{K1'}(P) = D_{K2'}(C)$ , try the keys on another  $(P', C')$

(4) If  $E_{K1'}(P') = D_{K2'}(C')$ ,  $(K1', K2') = (K1, K2)$  with high probability

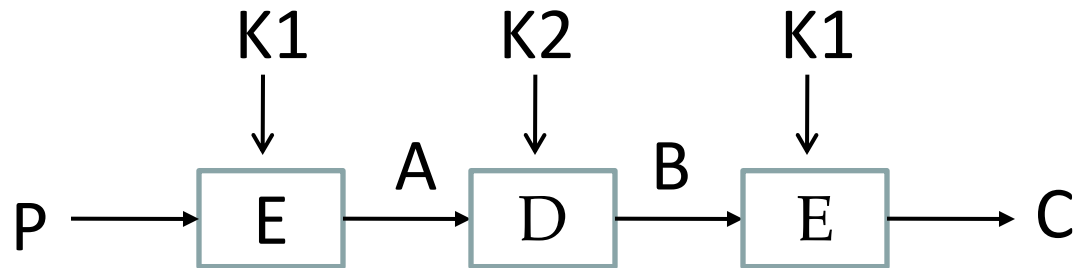
Takes  $2 \times 2^{56} = 2^{57}$  steps; not much more than attacking 1-DES.

# Triple-DES with Two-Keys

- hence must use 3 encryptions
  - would seem to need 3 distinct keys
- In practice:  $C = E_{K_1}(D_{K_2}(E_{K_1}(P)))$ 
  - Also referred to as EDE encryption
- Reason:
  - if  $K_1=K_2$ , then 3DES = 1DES. Thus, a 3DES software can be used as a single-DES.
- Standardized in ANSI X9.17 & ISO8732
- No current known practical attacks
  - Q: What about the meet-in-the-middle attack?



# Meet-in-the-Middle Attack on 3DES



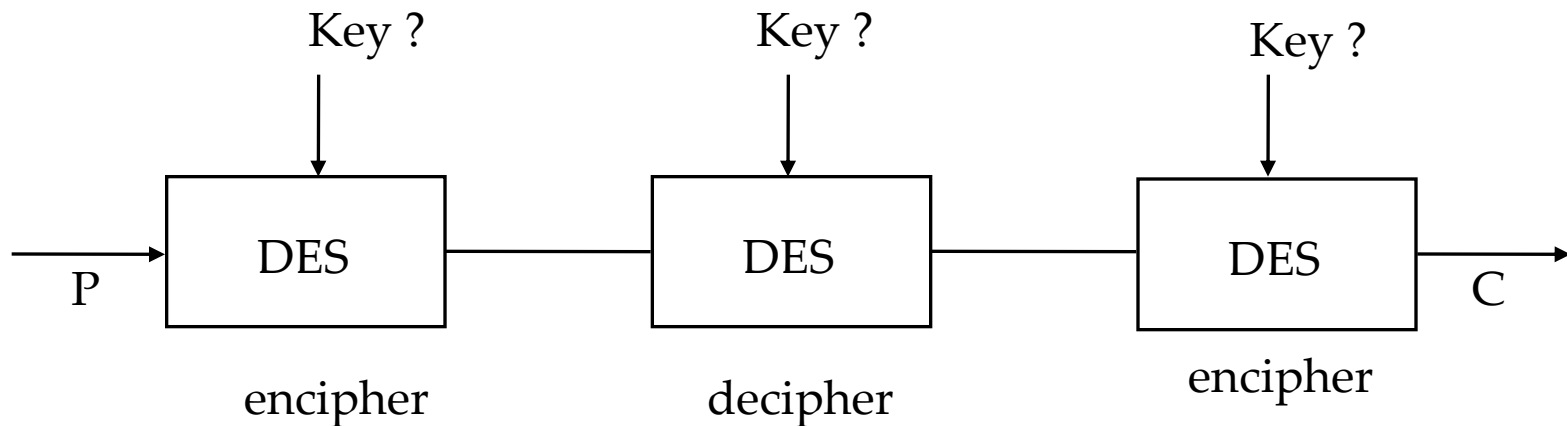
1. For each possible key for  $K1$ , encrypt  $P$  to produce a possible value for  $A$ .
2. Using this  $A$ , and  $C$ , attack the 2DES to obtain a pair of keys  $(K2, K1')$ .
3. If  $K1' = K1$ , try the key pair  $(K1, K2)$  on another  $(C', P')$ .
4. If it works,  $(K1, K2)$  is the key pair with high probability.
5. It takes  $O(2^{55} \times 2^{56}) = O(2^{111})$  steps on average.

# Triple-DES with Three-Keys

- Encryption:  $C = E_{K_3}(D_{K_2}(E_{K_1}(P)))$ .
- If  $K_1 = K_3$ , we have 3DES with 2 keys.
- If  $K_1 = K_2 = K_3$ , we have the regular DES.
- So, 3DES w/ 3keys is backward compatible with 3DES w/ 2 keys and with the regular DES
- Some internet applications have adopted 3DES with three keys.
  - E.g., PGP (pretty good privacy) and S/MIME (Secure/Multipurpose Internet Mail Extensions).

# Triple-DES

- Triple DES



With **two** keys:  $E_{K_1}(D_{K_2}(E_{K_1}(M))) = C$

With **three** keys:  $E_{K_1}(D_{K_2}(E_{K_3}(M))) = C$

# AES (Advanced Encryption Standard)

# AES

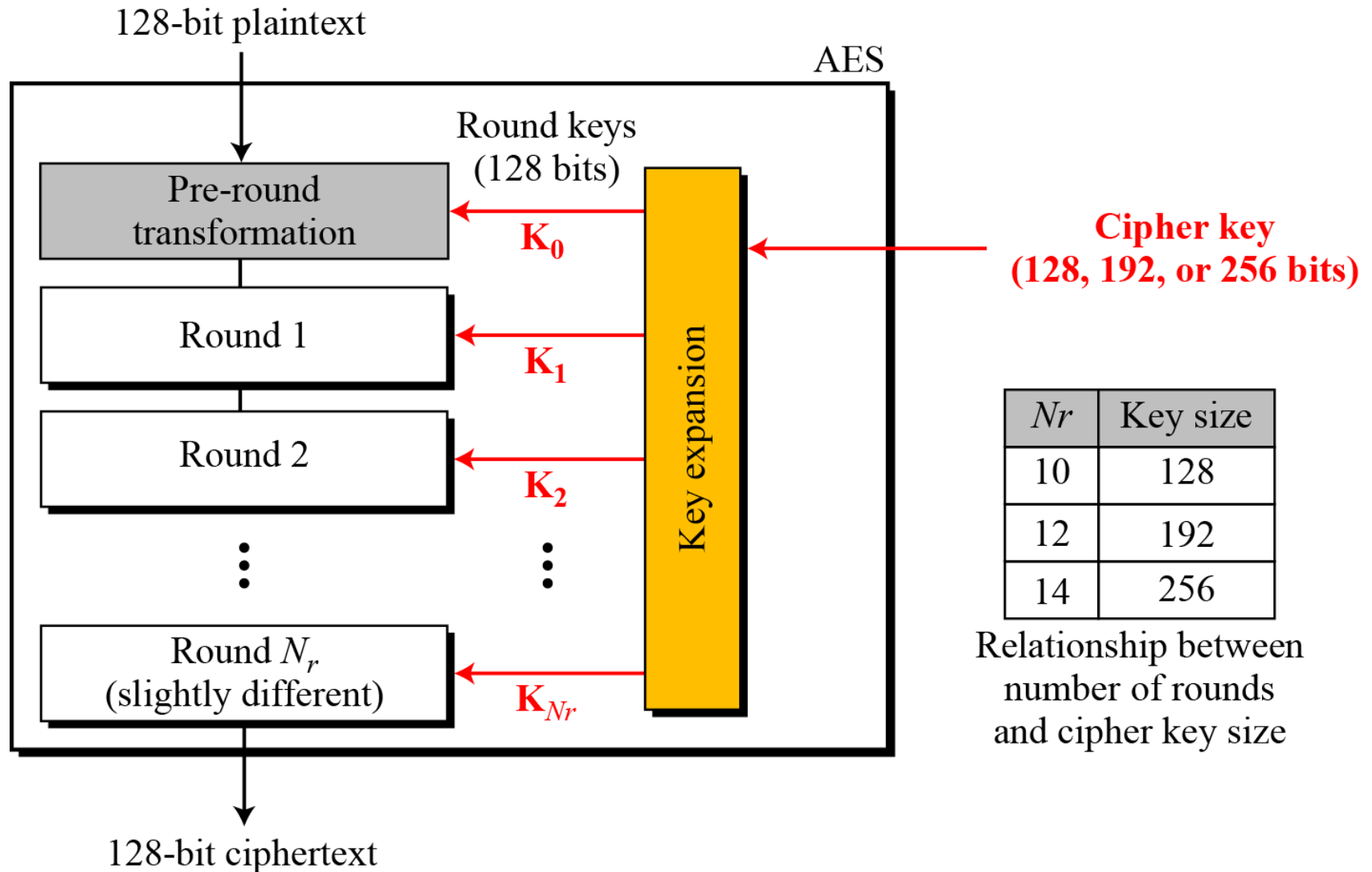
- DES cracked, Triple-DES slow: what next?
- 1997 NIST called for algorithms
- Final five
  - Rijndael (Two Belgians: Joan Daemen, Vincent Rijmen),
  - Serpent(Ross Anderson),
  - Twofish(Bruce Schneier),
  - RC6(Don Rivest, Lisa Yin),
  - MARS (Don Coppersmith, IBM)
- 2000 Rijndael won
- 2002 Rijndael became AES

# Overview of AES

- Based on a design principle known as *substitution-permutation network (SPN)*
- Block length is limited to **128** bit
- The **key size** can be independently specified to **128, 192 or 256** bits

Key size (words/bytes/bits)	4/16/ <b>128</b>	6/24/ <b>192</b>	8/32/ <b>256</b>
Number of rounds	<b>10</b>	<b>12</b>	<b>14</b>
Expanded key size (words/byte)	44/176	52/208	60/240

# General design of AES encryption cipher

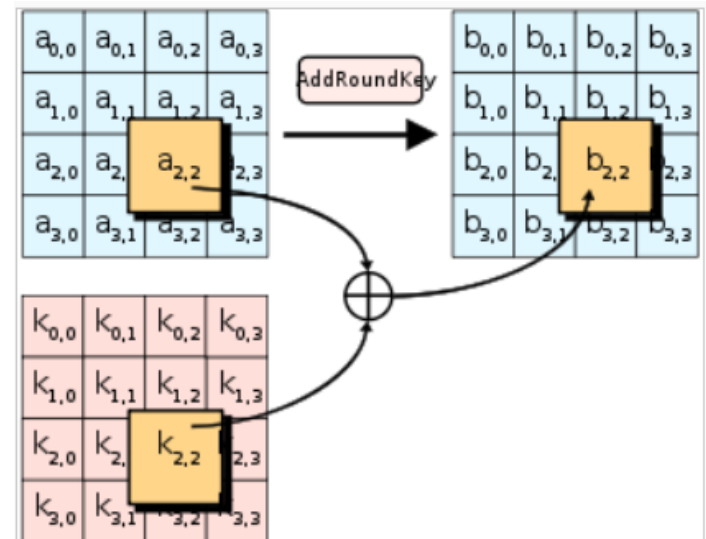
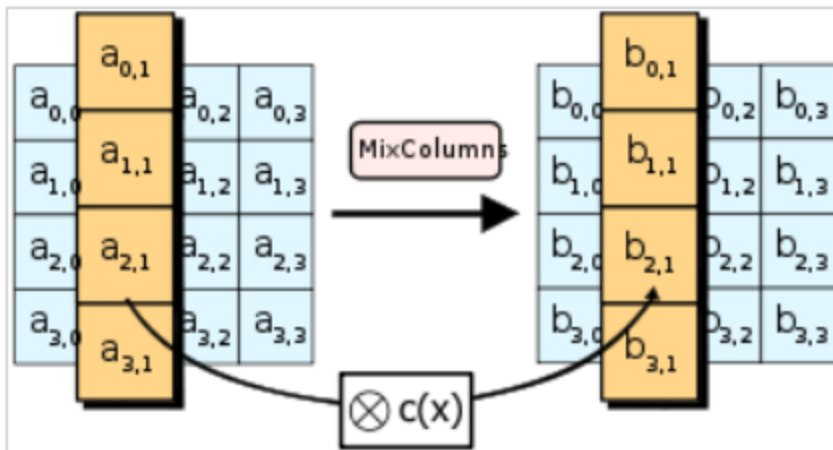
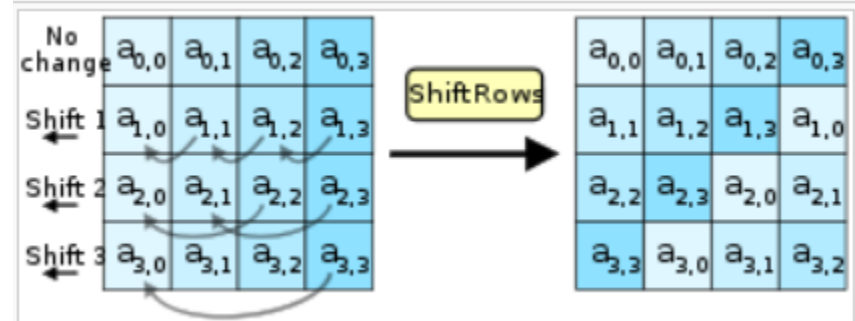
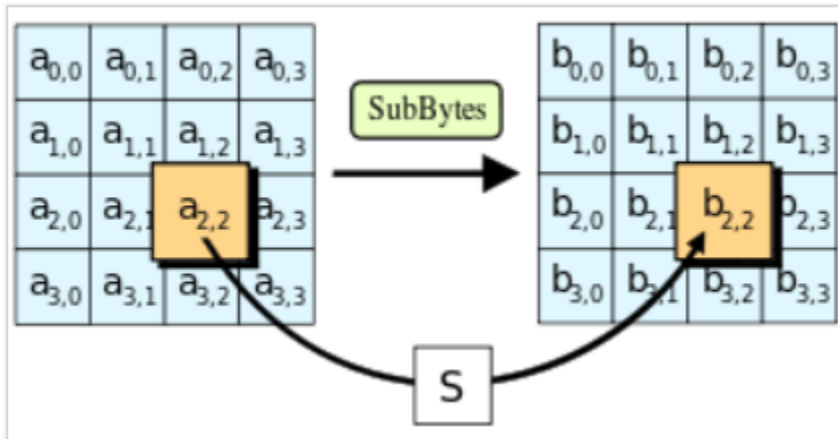


# AES

- Each round uses 4 functions
  - ByteSub (nonlinear layer) :
    - referred to as an S-box; byte-by-byte substitution
  - ShiftRow (linear mixing layer)
    - A simple permutation row by row
  - MixColumn (nonlinear layer)
    - A substitution that alters each byte in a column as function of all of the bytes in column
  - AddRoundKey (key addition layer)
    - A simple bitwise XOR of the current block with a portion of the expanded key



# AES 4 Steps



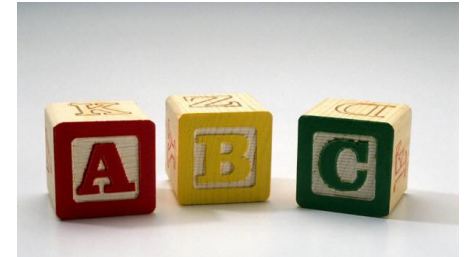
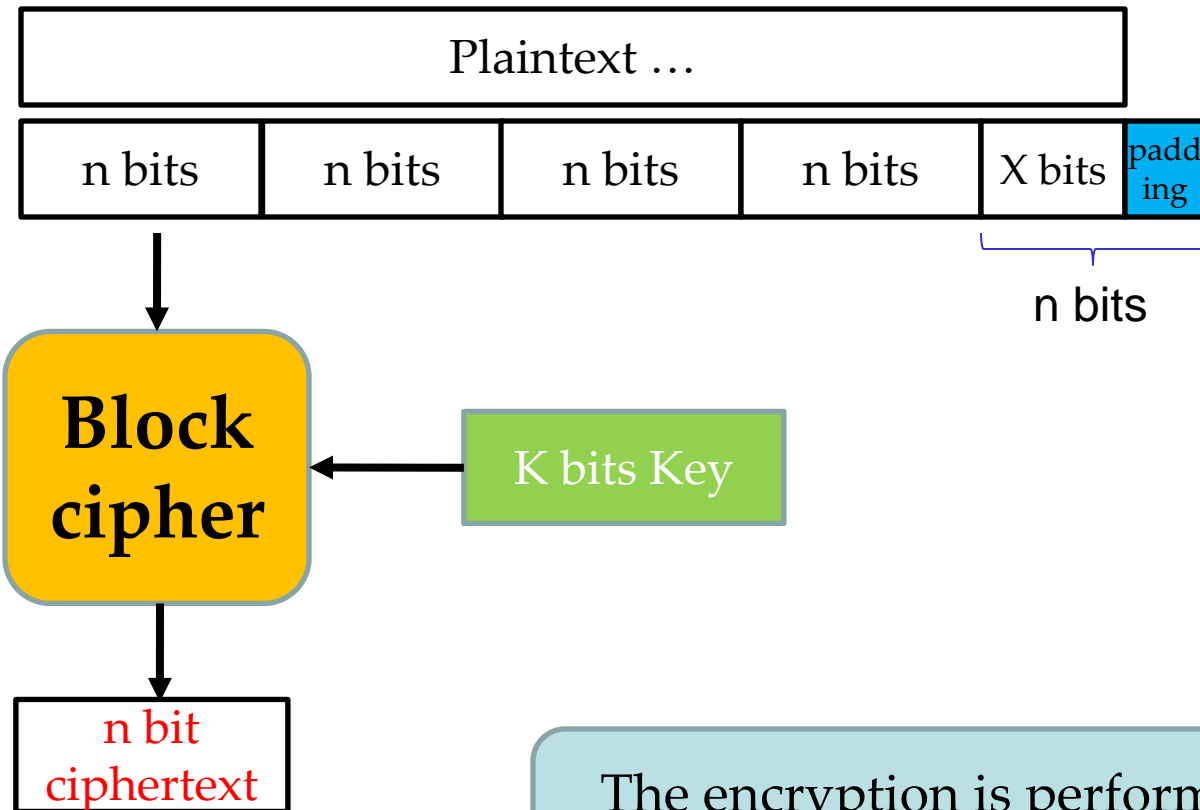
# DES vs. AES

	DES	AES
Date	1976	1999
Block size	64	128
Key length	56	128, 192, 256
Number of rounds	16	10,12,14
Encryption primitives	Substitution, permutation	Substitution, shift, bit mixing
Cryptographic primitives	Confusion, diffusion	Confusion, diffusion
Structure	Feistel	SPN( substitution-permutation network)
Design	Open	Open
Design rationale	Closed	Open
Selection process	Secret	Secret, but accept open public comment
Source	IBM, enhanced by NSA	Independent cryptographers

# Modes of operation

Q: If block size is bigger than 64 bits in case of using DES?

# Block cipher



The encryption is performed using one of the **operation modes**

Common block sizes:  
 $n = 64, 128, 256$  bits

Common key sizes:  
 $k = 40, 56, 64, 80, 128, 168, 192, 256$  bits

# Modes of Operation

- block ciphers encrypt fixed size blocks
  - e.g., DES encrypts 64-bit blocks with 56-bit key
- need some way to en/decrypt arbitrary amounts of data in practice
- **ANSI X3.106-1983 Modes of Use** (now FIPS 81) defines 4 possible modes
- subsequently 5 defined for AES & DES
- have **block** and **stream** modes

# Modes of Operation

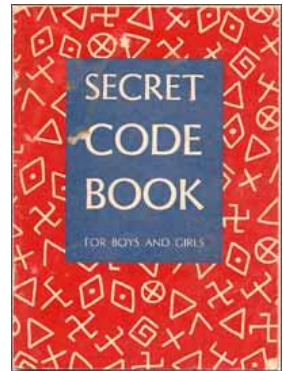
- **ECB** – Electronic Code Book
- **CBC** – Cipher Block Chaining **Most popular**
- **OFB** – Output Feed Back
- **CFB** – Cipher Feed Back
- **CTR** - Counter

# Electronic Codebook Book (ECB)

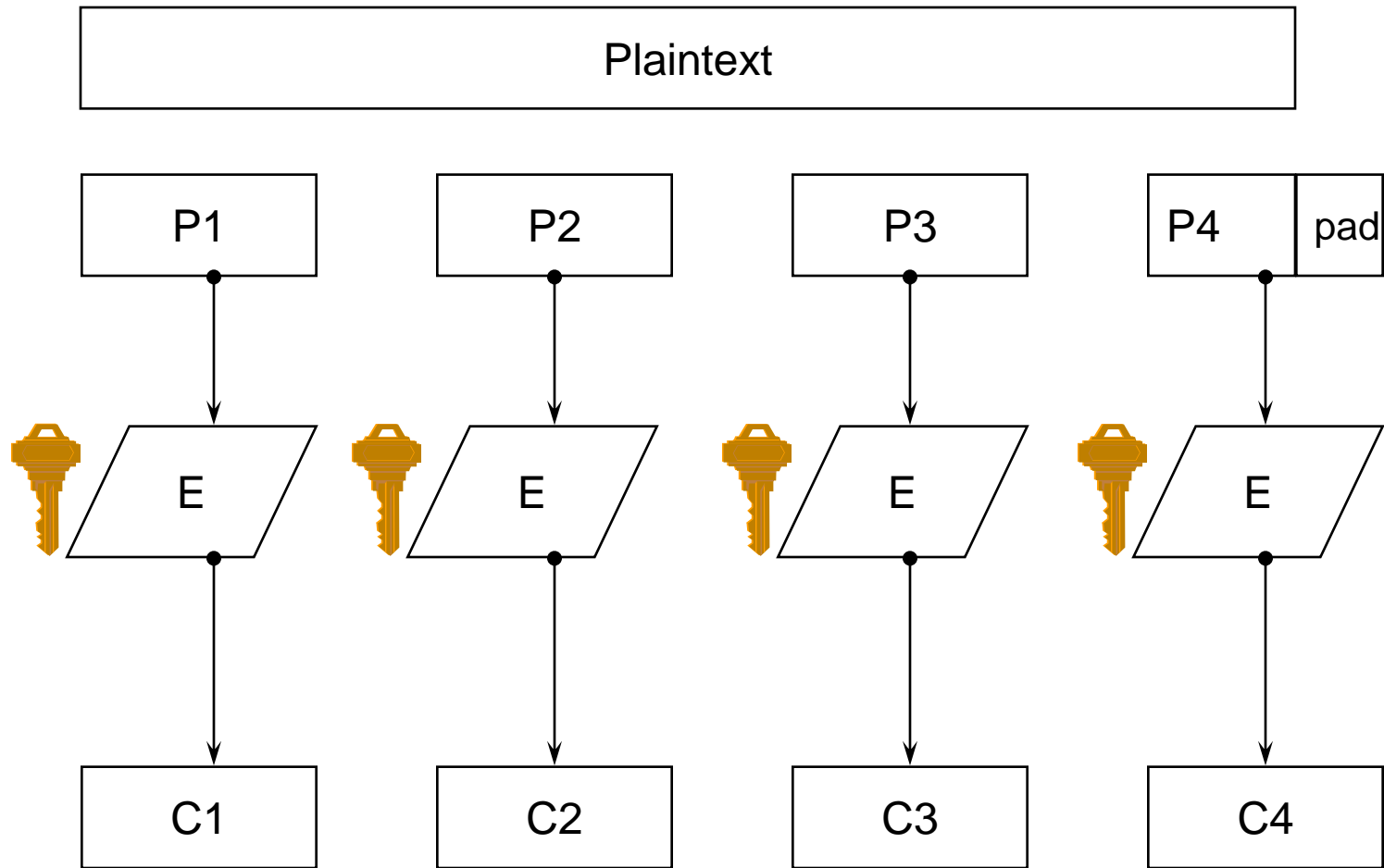
- Message (plaintext) is broken into independent blocks
- Each block is encrypted **independently** of the other blocks

$$C_i = \text{DES}_{K1}(P_i)$$

- Each block is a value which is substituted, and then encrypted like using a codebook.
  - If the same message (e.g., your IRD #) is encrypted (with the same key) and sent twice, their ciphertexts are the same.
- uses: secure transmission of single values



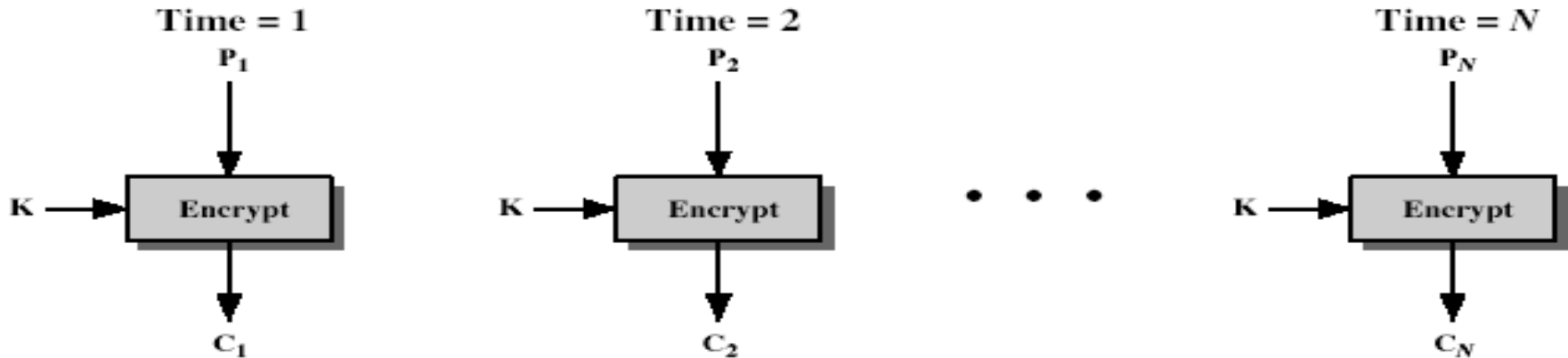
# Electronic Codebook Book mode



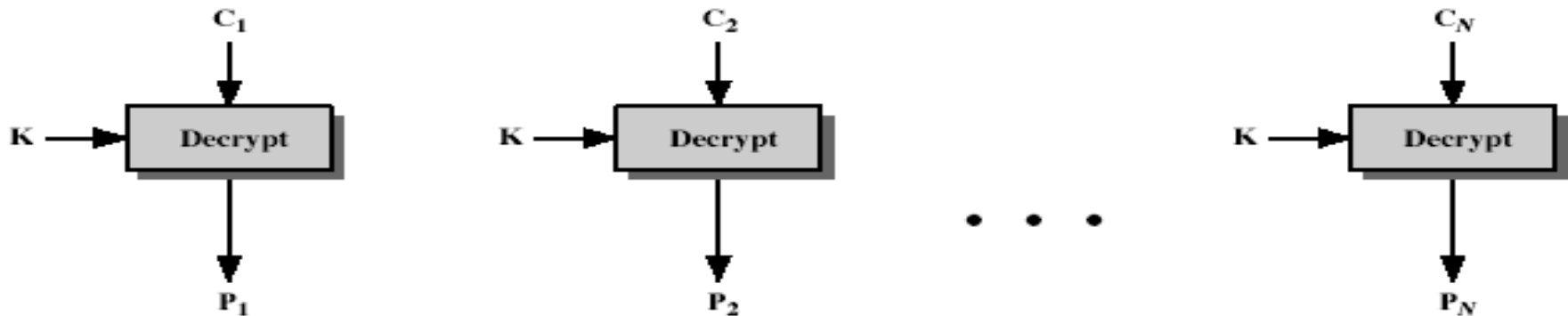
- Pad last block, if necessary



# ECB (both encryption/decryption)



(a) Encryption



(b) Decryption

Decryption

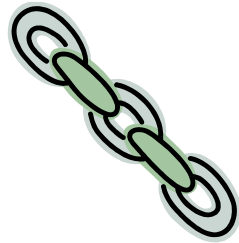
# Advantages and Limitations of ECB

- Message repetitions may show in ciphertext
  - if aligned with message block
  - particularly with data such graphics
  - or with messages that change very little, which become a **code-book analysis** problem
- Weakness is due to the encrypted message blocks being independent
- Main use is sending a few blocks of data

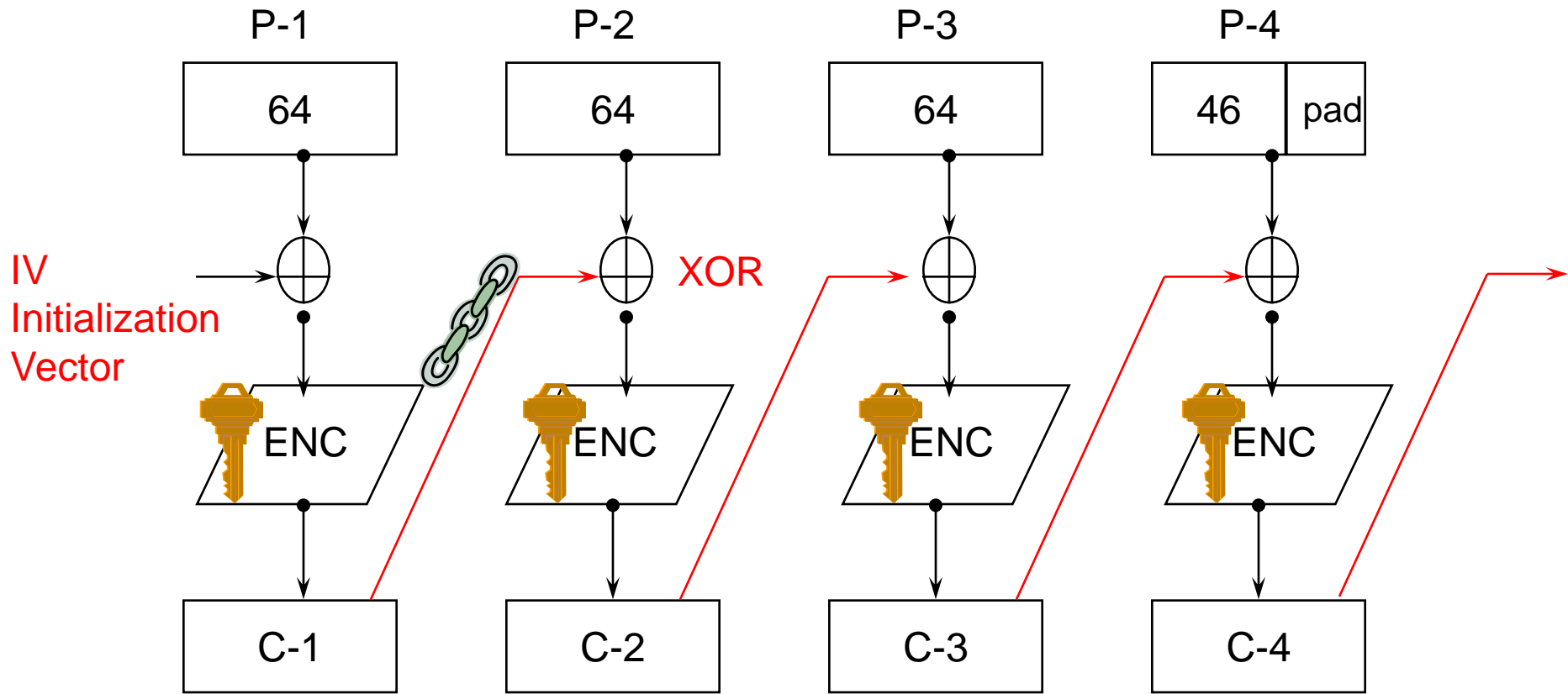
Any ideas to overcome the ECB  
mode?

# Cipher Block Chaining (CBC)

- message is broken into blocks
  - linked together in encryption operation
  - each previous cipher blocks is chained with current plaintext block
  - use Initial Vector (IV) to start process
- $$C_i = \text{DES}_{K1}(P_i \text{ XOR } C_{i-1})$$
- $$C_{-1} = \text{IV}$$
- uses: general block oriented transmission
    - e.g., IPsec uses 3DES-CBC, AES-CBC

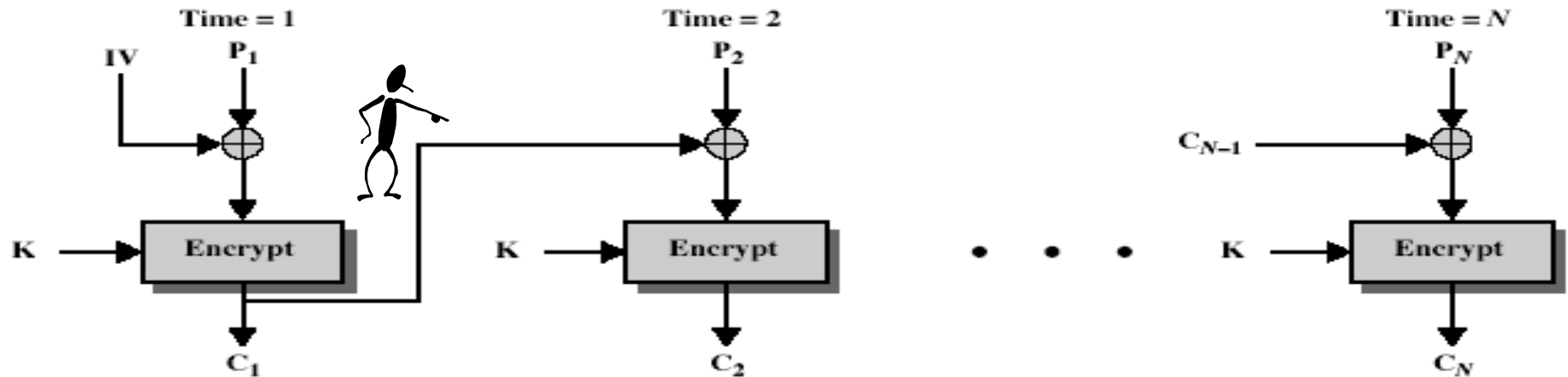


# Cipher Block Chaining (CBC)

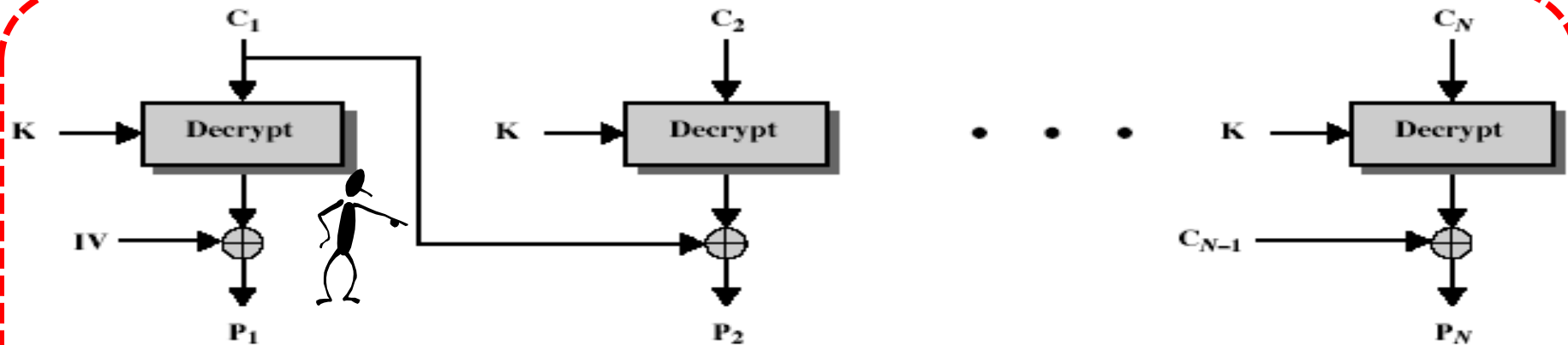


- Pad last block, if necessary
- Random Block called **IV** is required to be random/pseudo random.

# Cipher Block Chaining (CBC) : E/D



(a) Encryption

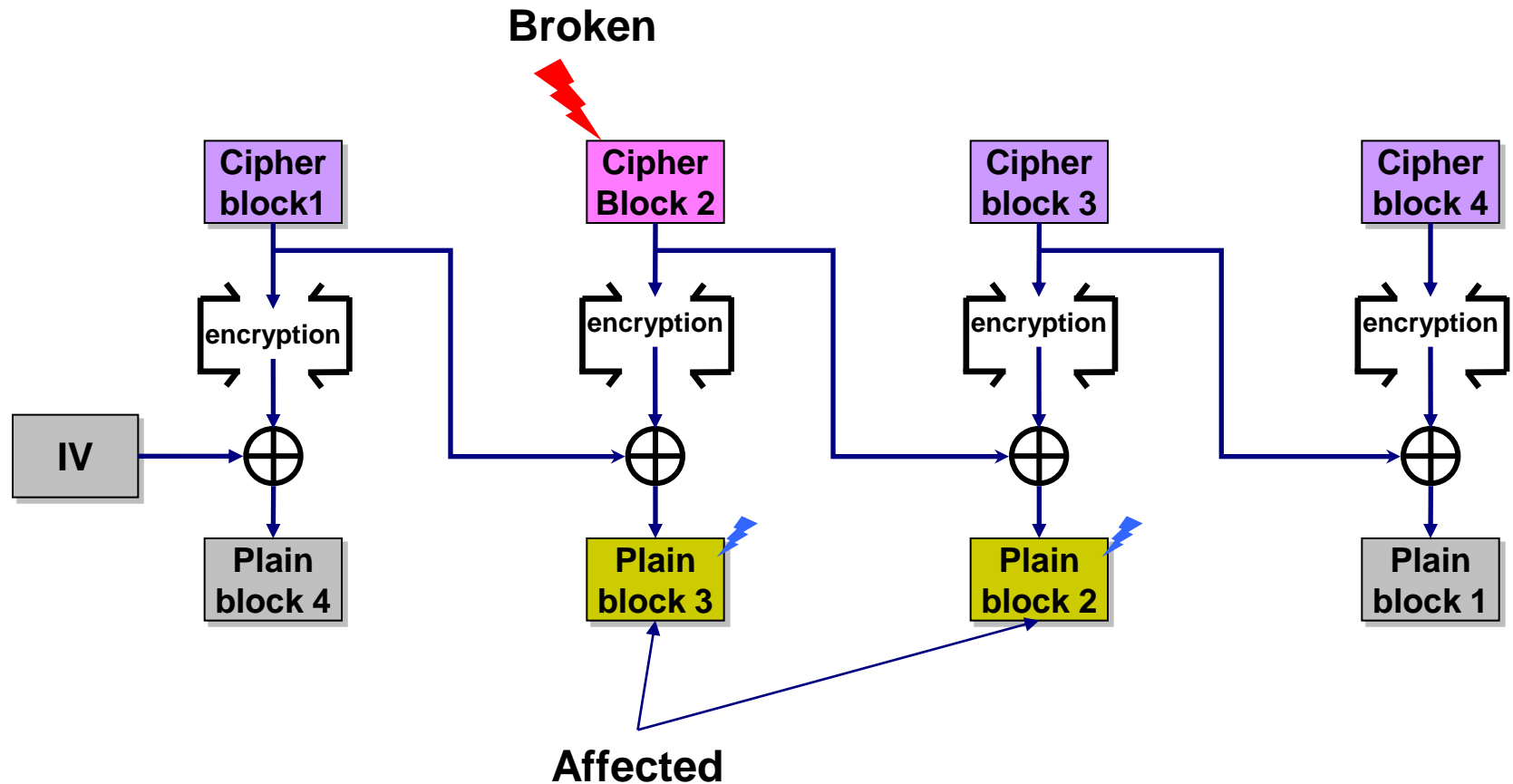


(b) Decryption

# Advantages and Limitations of CBC

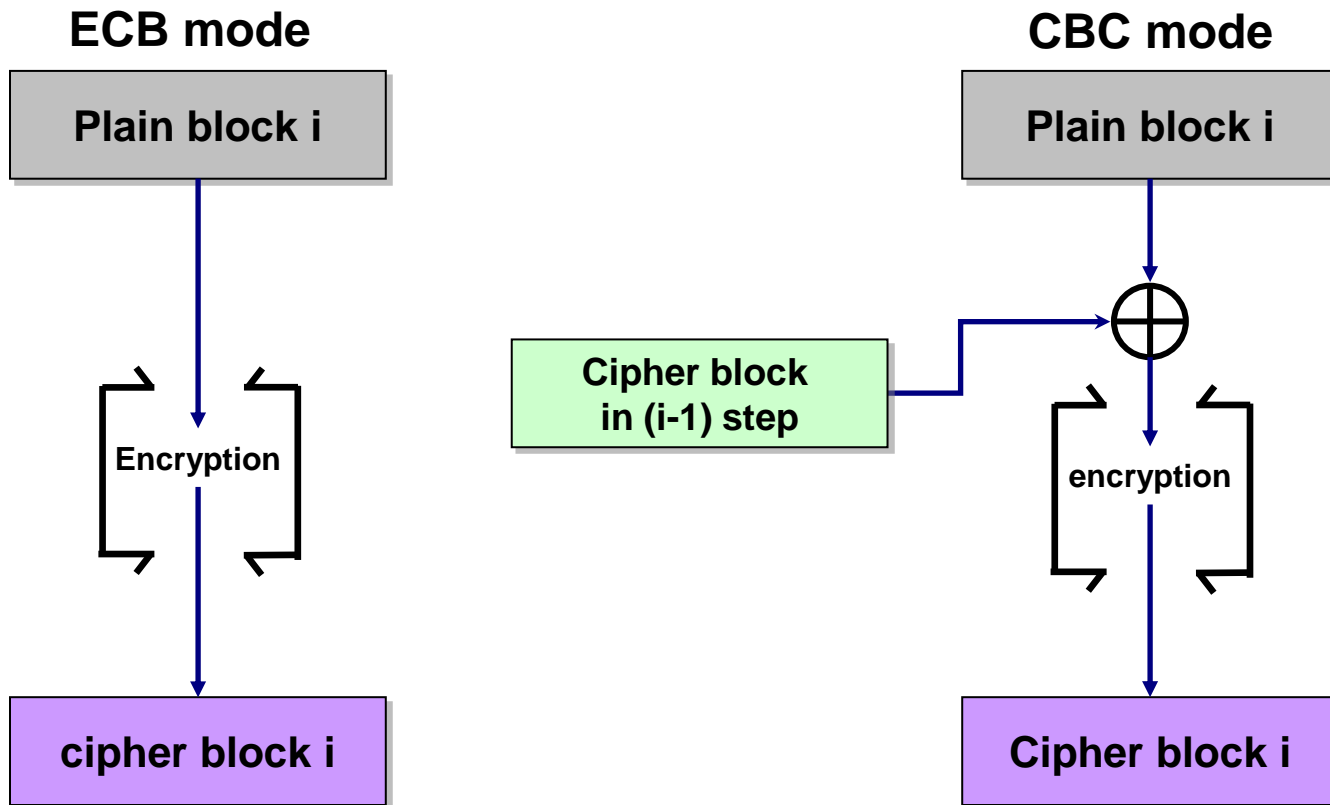
- A ciphertext block depends on **all** blocks before it
- So, repeated plaintext blocks are encrypted differently.
- need **Initialization Vector (IV)**
  - must be known to sender & receiver
  - if sent in clear, attacker can change bits of first block, and change **IV** to compensate, hence **IV** must either be a fixed value (Integrity of **IV** should be guaranteed)
  - or must be sent encrypted in **ECB** mode before rest of message

# Error propagation in CBC





# ECB vs. CBC mode



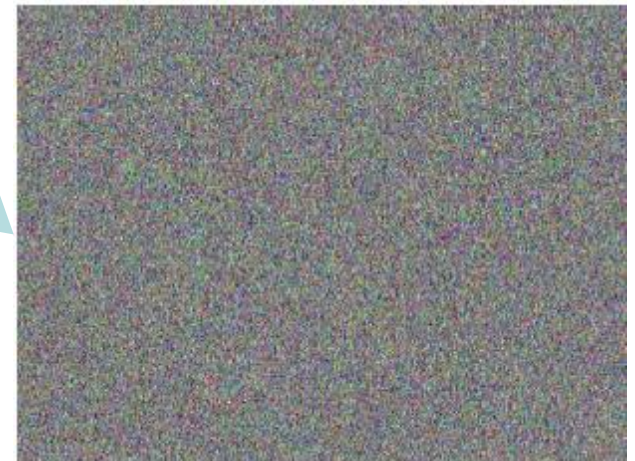
# ECB vs. CBC mode



ECB



CBC



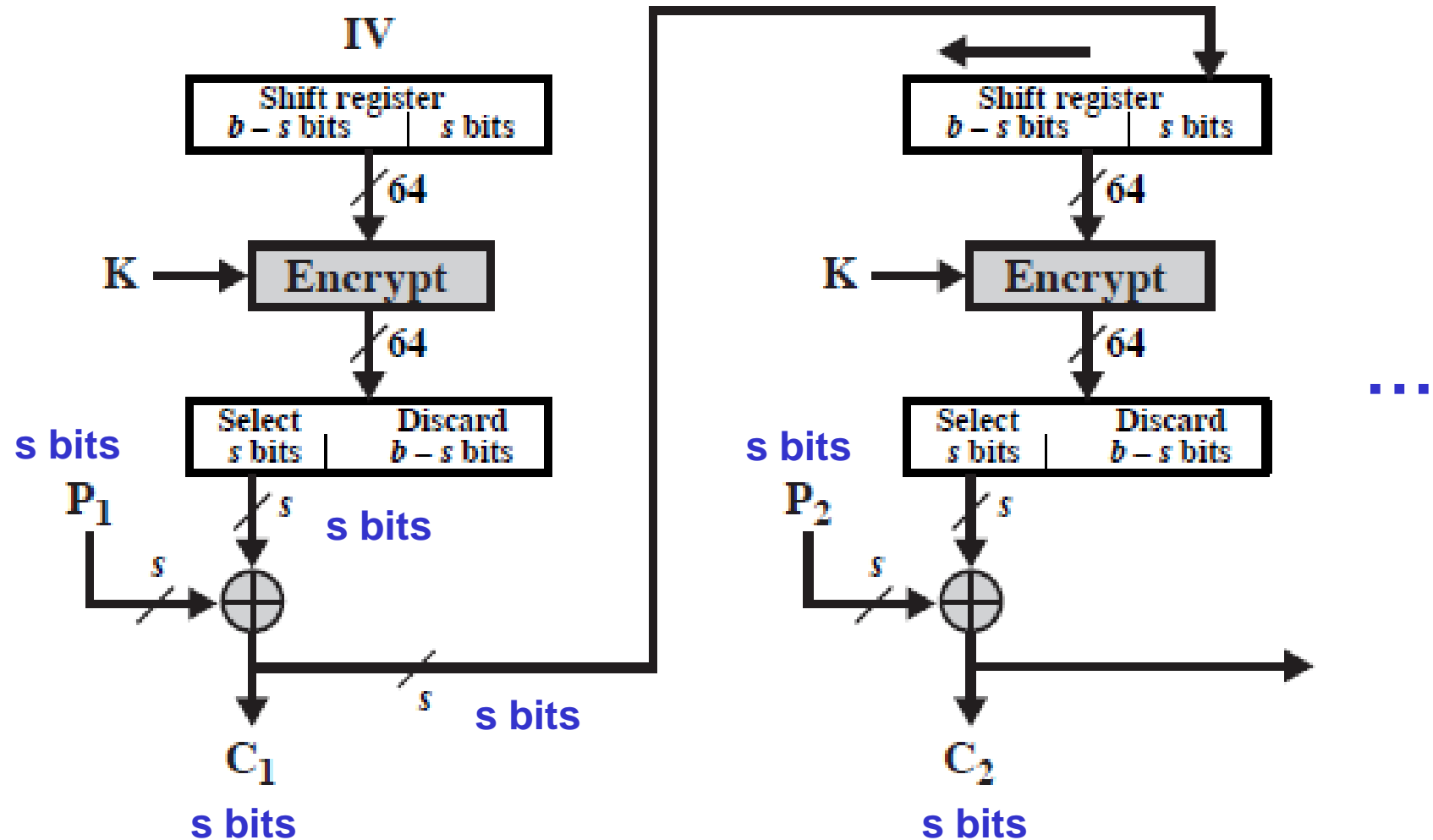
# Cipher Feed back (CFB) Mode

- The plaintext is divided into segments of  $s$  bits (where  $s \leq \text{block-size}$ ):  $P_1, P_2, P_3, P_4, \dots$
- Encryption is used to generate a sequence of keys, each of  $s$  bits:  $K_1, K_2, K_3, K_4, \dots$
- The ciphertext is  $C_1, C_2, C_3, C_4, \dots$ , where
$$C_i = P_i \oplus K_i$$

# Cipher Feed back (CFB) Mode

- Uses cipher block used in the previous step as input of cipher in the next step
- What does it mean “feedback”?
  - Cipher is used as input of the cipher

# Cipher Feed Back (CFB): Encryption

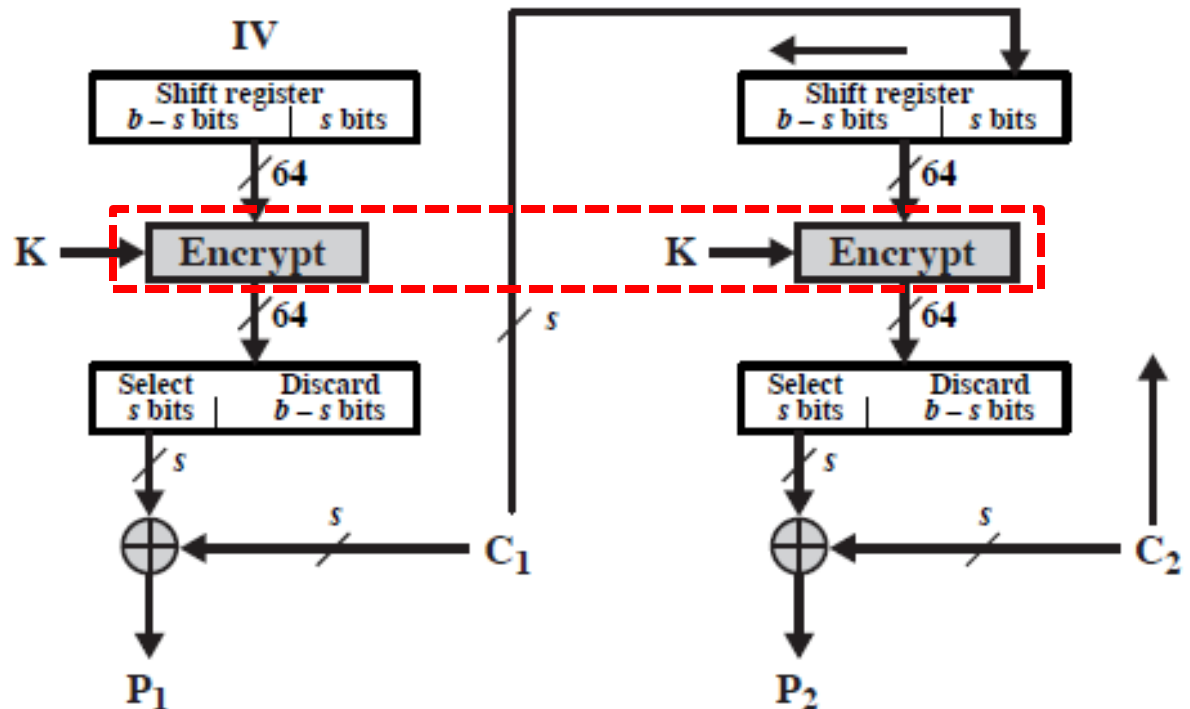


# Cipher Feed Back (CFB): Decryption

- Generate key stream  $K_1, K_2, K_3, K_4, \dots$  the same way as for encryption.
- Then decrypt each ciphertext segment as:

$$P_i = C_i \oplus K_i$$

It does not decrypt  
but encrypt

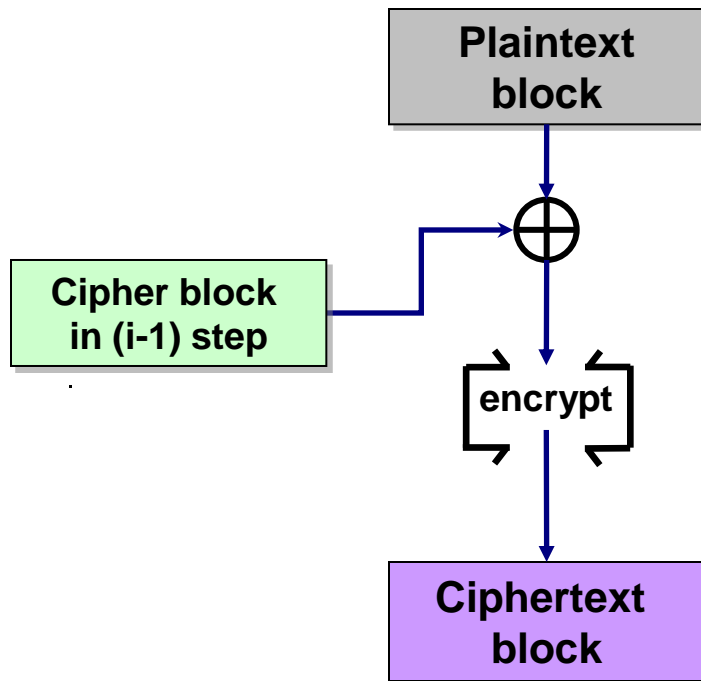


# Cipher Feed Back (CFB)

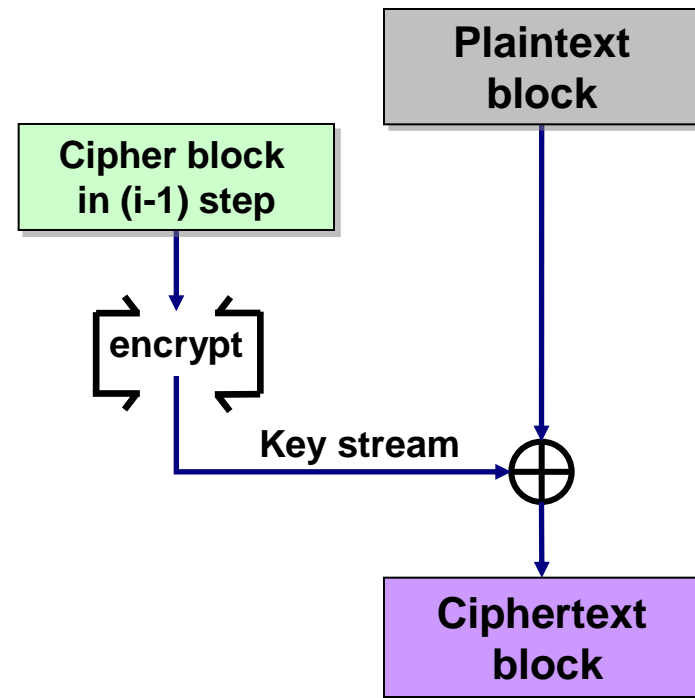
- The block cipher is used as a **stream cipher**.
- Appropriate when data arrives in bits/bytes.
  - $s$  can be any value; a common value is  $s = 8$ .
  - standard allows any number of bit (1, 8, 64 or 128 etc) to be feed back denoted CFB-1, CFB-8, CFB-64, CFB-128 etc
- A ciphertext segment depends on the current and all preceding plaintext segments.
- A corrupted ciphertext segment during transmission will affect the current and next several plaintext segments.

# CBC vs. CFB

## CBC mode



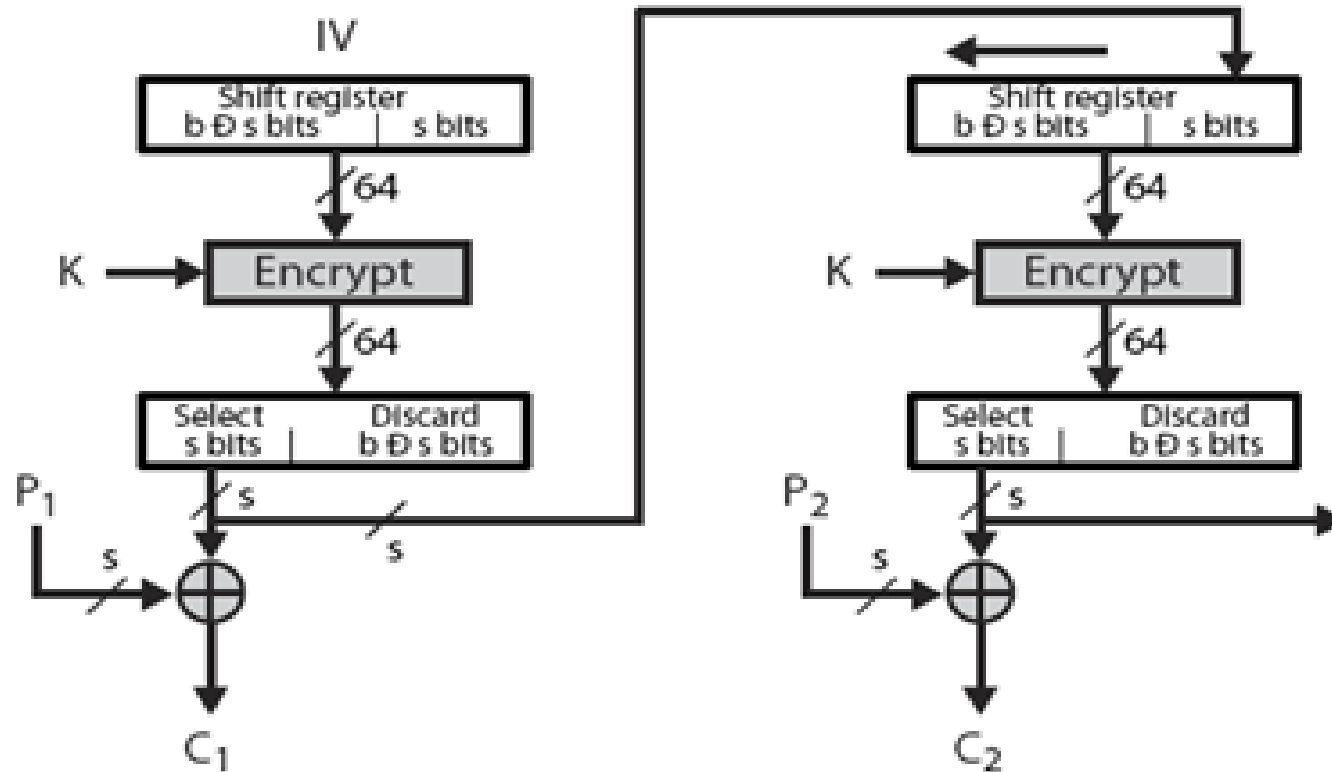
## CFB mode





# Output Feed Back (OFB) mode

OFB



# Output Feed Back (OFB) mode

- message is treated as a stream of bits (s bits)
- **output of cipher** is added to message
- **output is then feed back**
- feedback is independent of message
- can be computed in advance

$$C_i = P_i \text{ XOR } O_i$$

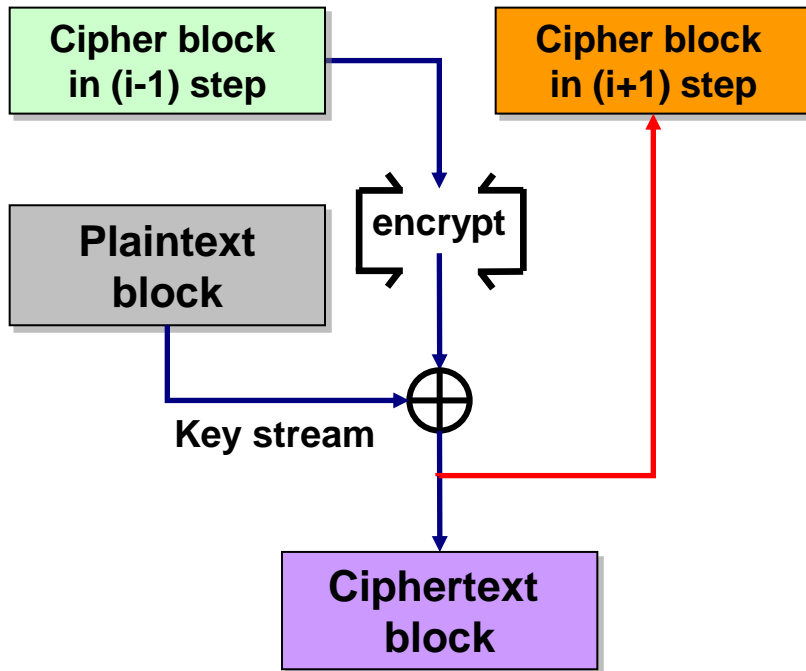
$$O_i = \text{DES}_{K1}(O_{i-1})$$

$$O_{-1} = \text{IV}$$

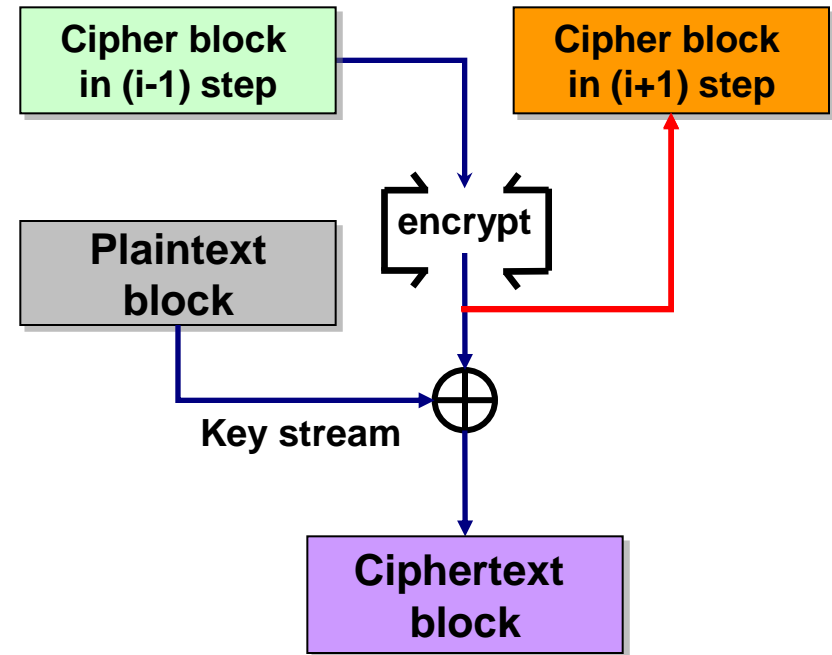
- uses: stream encryption on noisy channels (e.g., satellite TV transmissions etc)

# CFB vs. OFB

CFB mode

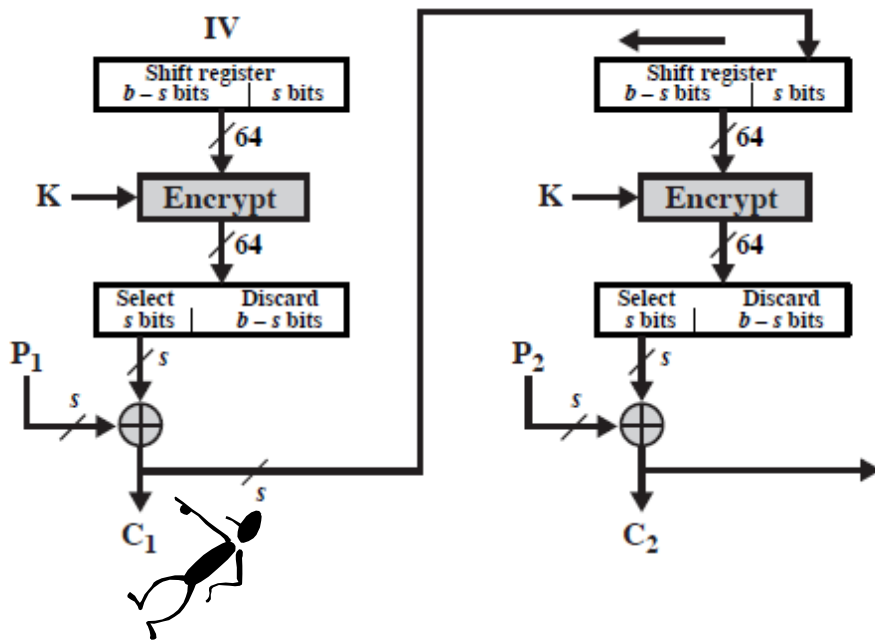


OFB mode

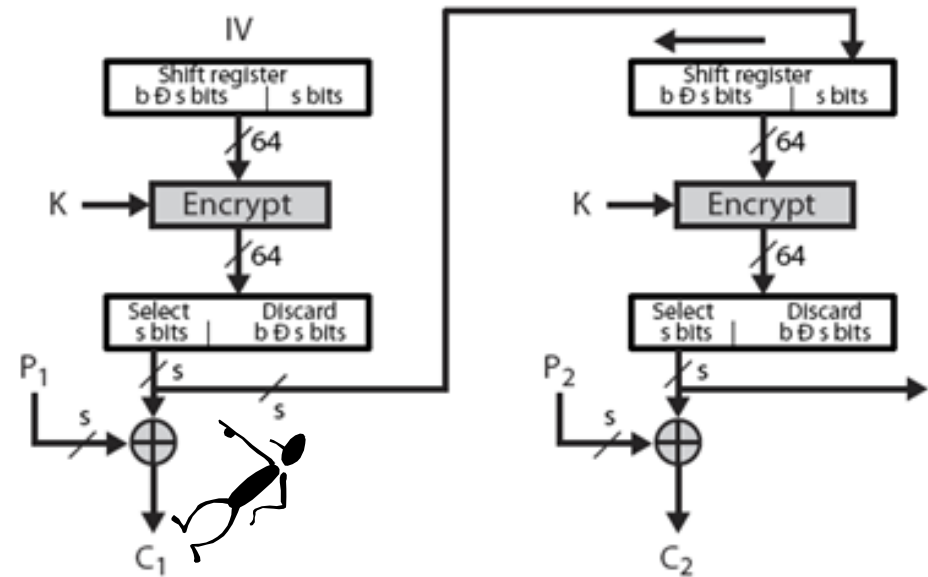


# CFB vs. OFB (contd)

CFB



OFB



# Advantages and Limitations of OFB

- bit errors do not propagate
- more vulnerable to message stream modification
- a variation of a Vernam cipher
  - hence must **never** reuse the same sequence (key+IV) ;
  - otherwise 2 ciphertexts can be combined, cancelling these bits
- sender & receiver must remain in sync

Vernam cipher: the plaintext is XORed with a random or pseudorandom stream of data (the "keystream") of the same length to generate the ciphertext

# Counter (CTR)

- a “new” mode, though proposed early on
- similar to OFB but encrypts **counter value** rather than any feedback value
- must have a different key & counter value for every plaintext block (never reused)

$$C_i = P_i \text{ XOR } O_i$$

$$O_i = \text{DES}_{K1}(i)$$

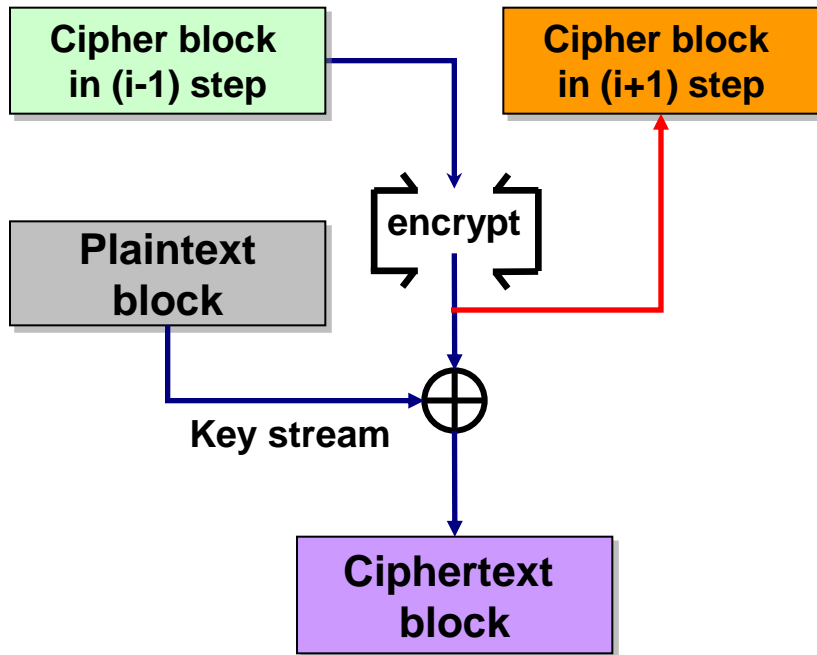
- uses: high-speed network encryptions
  - e.g., AES-CTR (i.e., AES in CTR mode)

OCB (Offset Codebook Mode) (Counter Mode)

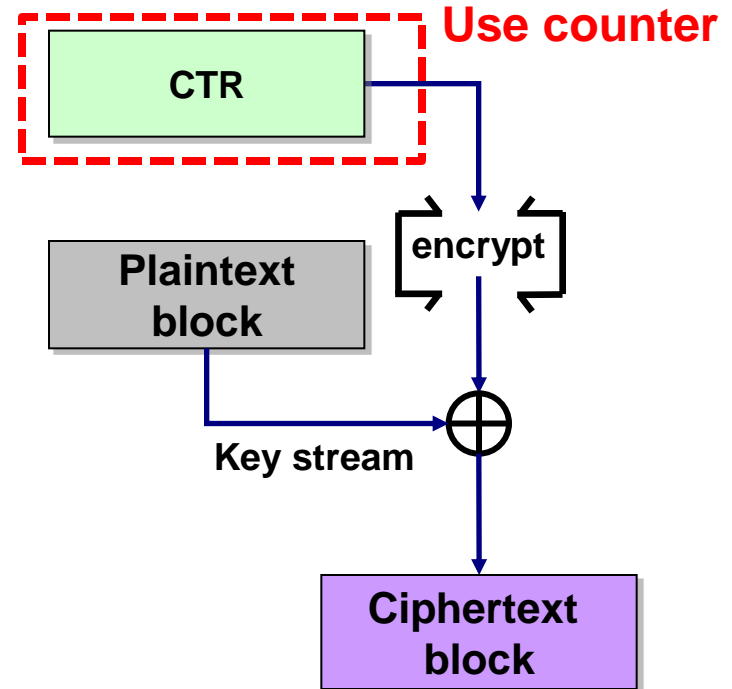
[new] Ref: P Rogaway, OCB Mode, <http://csrc.nist.gov/encryption/aes>

# OFB vs. CTR mode

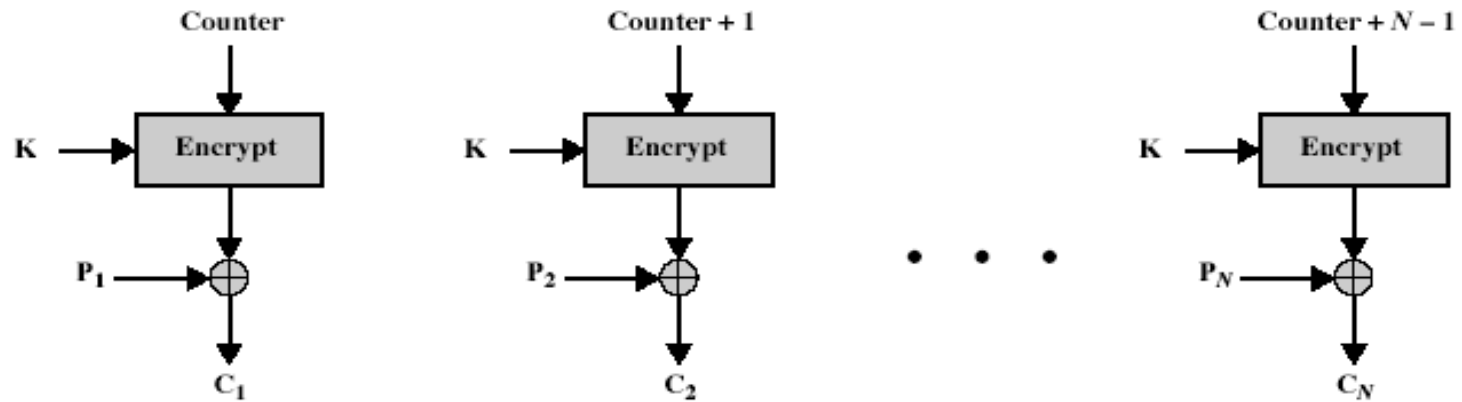
OFB mode



CTR mode

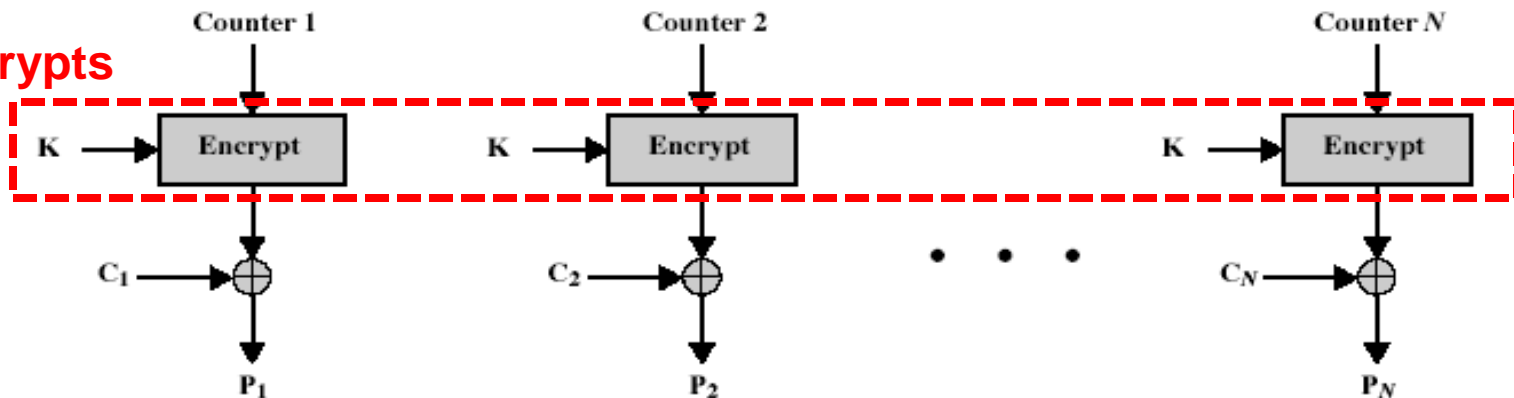


# Counter (CTR)



(a) Encryption

It encrypts



(b) Decryption


Q: how to generate counter?



# CTR

- A counter T is initialized to some **IV (nonce)** and then incremented by 1 for each subsequent plaintext block.
- Counter example (128 bits/16 bytes).

**66 1F 98 CD 37 A3 8B 4B 00 00 00 00 00 00 00 01**

  
**Nonce** (an arbitrary number )      **Block number**

- 66 1F 98 CD 37 A3 8B 4B 00 00 00 00 00 00 00 01 (initial)
- 66 1F 98 CD 37 A3 8B 4B 00 00 00 00 00 00 00 02 (counter 2)
- 66 1F 98 CD 37 A3 8B 4B 00 00 00 00 00 00 00 03 (counter 3)
- 66 1F 98 CD 37 A3 8B 4B 00 00 00 00 00 00 00 04 (counter 4)
- $\vdots$

# Advantages and Limitations of CTR

- Needs only the encryption algorithm (so do CFB and OFB)
- Fast encryption/decryption;
  - blocks can be processed (encrypted or decrypted) in parallel in SW/HW; good for high speed links
- random access to encrypted data blocks
- provable security (good as other modes)
- but as in OFB, must ensure never reuse key/counter values, otherwise could break

# Modes of Operation: summary

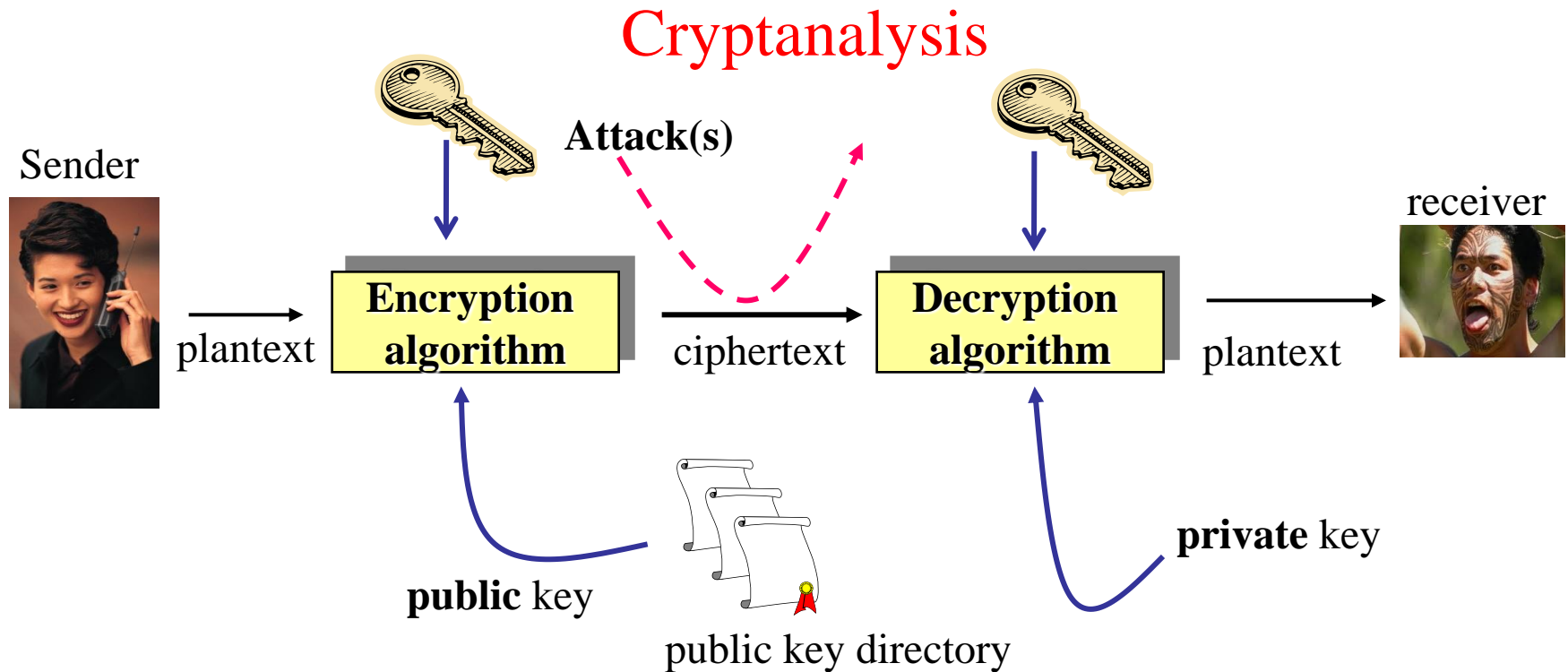
- **ECB** – Electronic Code Book    Don't use
- **CBC** – Cipher Block Chaining    Most popular,  
e.g., DES-CBC
- **OFB** – Output Feed Back
- **CFB** – Cipher Feed Back    } Use CTR
- **CTR** - Counter    e.g., AES-CTR

Q: What security objective does this provide?

A: Confidentiality

Q: How do we know the  
encryption (block cipher) is  
secure?

# Cryptanalysis



# Cryptanalysis (cont'd)

- objective to recover key not just message
- general approaches:
  - cryptanalytic attack
  - brute-force attack

# Breaking Ciphers

- **Ciphertext only** (COA, Known-ciphertext)
  - Attacker can only access to a set of ciphertext
- **Known plaintext** (KPA)
  - know/suspect plaintext & ciphertext
- **Chosen plaintext** (CPA)
  - select plaintext to be encrypted and obtain ciphertext
- **Chosen ciphertext**
  - select ciphertext and obtain plaintext under an unknown key
- **Chosen text**
  - select plaintext or ciphertext to en/decrypt

# Ciphertext-only attack

Known to attacker	$C_1, C_2, \dots, C_n$
Objective	1) $P_1, P_2, \dots, P_n$
	2) Key $K$
	3) Algorithm: $C_{n+1} \rightarrow P_{n+1}$

Ciphertexts generated using the same key


Find an algorithm that can decrypt any message encrypted using the key  $K$ .



# Known-plaintext attack

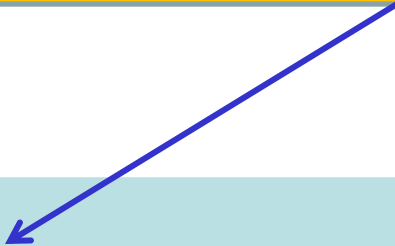
Known to attacker	$(P_1, C_1), (P_2, C_2), \dots, (P_n, C_n),$
Objective	1) Key $K$
	2) Algorithm: $C_{n+1} \rightarrow P_{n+1}$

Attacker  
**cannot** select  
these pairs



# Chosen-plaintext attack

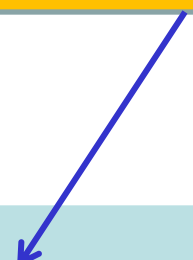
Attackers **can select**  $P_1, P_2, \dots, P_n$  before the attack begins and **cannot** obtain additional pair after the attack has begun.



Known to attacker	$(P_1, C_1), (P_2, C_2), \dots, (P_n, C_n),$
Objective	1) Key $K$
	2) Algorithm: $C_{n+1} \rightarrow P_{n+1}$

# Chosen-ciphertext attack

Attackers **can** select  $C_1, C_2, \dots, C_n$  before the attack begins.



Known to attacker	$(P_1, C_1), (P_2, C_2), \dots, (P_n, C_n),$
Objective	1) Key $K$
	2) Algorithm: $C_{n+1} \rightarrow P_{n+1}$

This attack is used against **public key algorithm**. Attacker can by itself generate the ciphertexts using the public key of the target.

# Result of Attacks

- Total break:

- found the **key**

Objective	1) Key K
	2) Algorithm: $C_{n+1} \rightarrow P_{n+1}$

- Global deduction:

- Was not successful in finding the key, but successful in finding **an algorithm** that can decrypt any ciphertexts of the target.

- Instance deduction:

- Obtained **some plaintexts** from some ciphertexts.

- Information deduction:

- Obtained **a partial bits** of plaintext of partial bits of the target key

# Secureness of an cipher

## ■ Computational secure

- **Cost** of breaking the cipher exceeds the value of the encrypted information (e.g., 1 million NZD cost vs. 1000 NZD secret)
- The **time** required to break the cipher exceeds the useful lifetime of the information (e.g., 1 month to break the all black's tactics)

## ■ Provably secure:

- the security of the system can be proven to be equivalent to a hard problem

## ■ Unconditional security

- Even if the attacker has infinite amount of computing resource, the attacker cannot succeed in cryptanalyzing the algorithm
- Only one-time pad is proven to be unconditionally secure

# Brute Force Search

- always possible to simply try every key
  - e.g., PIN number (0000)
- most basic attack, proportional to key size
- assume either know / recognise plaintext

Key Size (bits)	Number of Alternative Keys	Time required at 1 decryption/ $\mu$ s	Time required at $10^6$ decryptions/ $\mu$ s
32	$2^{32} = 4.3 \times 10^9$	$2^{31} \mu\text{s} = 35.8 \text{ minutes}$	2.15 milliseconds
56	$2^{56} = 7.2 \times 10^{16}$	$2^{55} \mu\text{s} = 1142 \text{ years}$	10.01 hours
128	$2^{128} = 3.4 \times 10^{38}$	$2^{127} \mu\text{s} = 5.4 \times 10^{24} \text{ years}$	$5.4 \times 10^{18} \text{ years}$
168	$2^{168} = 3.7 \times 10^{50}$	$2^{167} \mu\text{s} = 5.9 \times 10^{36} \text{ years}$	$5.9 \times 10^{30} \text{ years}$
26 characters (permutation)	$26! = 4 \times 10^{26}$	$2 \times 10^{26} \mu\text{s} = 6.4 \times 10^{12} \text{ years}$	$6.4 \times 10^6 \text{ years}$

Q: Is DES computationally secure?

Q: Why do we need public key  
encryptions?

